

1 **Improving Predictions of Stream CO₂ Concentrations and Fluxes using a Stream**
2 **Network Model: a Case Study in the East River Watershed, CO, USA**

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6 **Key Points:**

- 7 • We present a stream network model that accurately predicts stream $p\text{CO}_2$ and fluxes
8 through representation of physical hydrologic processes
- 9 • Inverse correlations between $p\text{CO}_2$ and atmosphere exchange velocities cause up to 13x
10 overestimates of river CO₂ fluxes from statistical upscaling
- 11 • Model-data comparisons suggest that internal CO₂ sources account for roughly half of
12 watershed CO₂ fluxes through hyporheic zone respiration
- 13

14 Abstract

15 Rivers and streams are an important component of the global carbon budget, emitting
16 CO₂ to the atmosphere. However, our ability to accurately predict carbon fluxes from stream
17 systems remains uncertain due to small scales of *p*CO₂ variability within streams (10⁰-10² m),
18 which make monitoring intractable. Here we incorporate CO₂ input and output fluxes into a
19 stream network advection-reaction model, representing the first process-based representation of
20 stream CO₂ dynamics at watershed scales. This model includes groundwater (GW) CO₂ inputs,
21 water column and benthic hyporheic zone (BZ) respiration, downstream advection, and
22 atmospheric exchange. We evaluate this model against existing statistical methods including
23 upscaling techniques and multiple linear regression models through comparisons to high-
24 resolution stream *p*CO₂ data collected across the East River Watershed in the Colorado Rocky
25 Mountains. The stream network model accurately captures topography-driven *p*CO₂ variability
26 and significantly outperforms multiple linear regressions for predicting *p*CO₂. Further, the model
27 provides estimates of CO₂ contributions from internal versus external sources and suggests that
28 streams transition from GW- to BZ-dominated sources between 3rd and 4th Strahler orders, with
29 GW and BZ accounting for 53 and 47% of CO₂ fluxes from the watershed, respectively. Lastly,
30 stream network model CO₂ fluxes are 5-13x times smaller than upscaling technique predictions,
31 largely due to inverse correlations between stream *p*CO₂ and atmosphere exchange velocities.
32 Taken together, the stream network model presented improves our ability to predict and monitor
33 stream CO₂ dynamics, and future applications to regional and global scales may result in a
34 significant downward revision of global flux estimates.

35 Plain Language Summary

36 Rivers and streams are an important part of the global carbon cycle, contributing carbon dioxide
37 to the atmosphere. However, the amount of carbon dioxide these systems contribute is
38 notoriously difficult to measure as it changes over short spatial scales. In this paper we present a
39 method of modeling carbon dioxide that uses the current understanding of sources, transport, and
40 reactions that carbon dioxide undergoes in these systems. This model is compared to previous
41 methods of predicting carbon dioxide contributions from streams, using data collected in the East
42 River Watershed in the Colorado Rocky Mountains. We find that the process-based model
43 presented here is more accurate than current methods of predicting carbon dioxide contributions
44 from rivers to the atmosphere. Furthermore, the model suggests that carbon dioxide produced

45 within the stream corridor, as opposed to soil and groundwater sources, contributed roughly half
46 of watershed stream carbon dioxide fluxes. Finally, we show that previous methods for modeling
47 stream carbon dioxide overestimate watershed fluxes by as much as 13x; therefore, the
48 application of a process-based model to larger systems may result in a large decrease in global
49 estimates of stream carbon dioxide fluxes.

50

51 **1 Introduction**

52 Inland waters have been recognized as an important component of the carbon cycle,
53 connecting terrestrial carbon (C) to the oceans and atmosphere (Cole et al., 2007). Among inland
54 waters, rivers and streams are the largest contributors of CO₂ accounting for 70% of total fluxes
55 (Raymond et al., 2013). Within rivers and streams, headwater are often considered hotspots of
56 CO₂ evasion contributing roughly 30% of the 0.7 - 3.88 Pg of C yr⁻¹ inland waters emit to the
57 atmosphere (Drake et al., 2018; Lauerwald et al., 2015; Marx et al., 2017; Raymond et al., 2013).
58 Currently efforts to monitor and predict CO₂ fluxes depend on accurate stream *p*CO₂ estimates
59 derived from pH, temperature, and alkalinity (Marx et al., 2017; Raymond et al., 2013) or using
60 direct measurements (Sawakuchi et al., 2017). However, these types of measurements are not
61 feasible to deploy at the scales (10⁰-10² m) required to capture the spatial variability of *p*CO₂
62 within stream networks. Due to this inability to measure stream CO₂ with adequate resolution,
63 global fluxes remain highly uncertain and are continuously revised using new statistical scaling
64 models and river data products (Allen & Pavelsky, 2018; Horgby et al., 2019b; Sawakuchi et al.,
65 2017). While the processes that control CO₂ variability and fluxes along stream networks are
66 relatively well characterized, current flux budgets rely exclusively on empirical and statistical
67 upscaling or modeling efforts.

68 Specifically, efforts to quantify large-scale stream CO₂ fluxes generally employ one of
69 two methodologies: statistical upscaling or multiple linear regression analysis. Upscaling efforts
70 typically use statistical distributions of *p*CO₂ observations, often categorized by Strahler stream
71 order, and apply these to unmeasured regions (Butman & Raymond, 2011; Raymond et al.,
72 2013). Alternatively, a number of studies have used statistical regressions to predict *p*CO₂ based
73 on readily available environmental variables such as elevation, soil organic carbon content,
74 discharge (Q), and areal wetland extent (Borges et al., 2015; Horgby et al., 2019b; Rocher-Ros et

75 al., 2019). In both cases, fluxes are then calculated based on estimated $p\text{CO}_2$ and calculated gas
76 transfer velocities (k) from stream turbulence and geomorphology (e.g., Raymond et al., 2012;
77 Ulseth et al., 2019). While these methods allow for large-scale flux estimates from relatively
78 coarse resolution observations, recent work has suggested that associated flux estimates involve
79 significant uncertainty. These uncertainties include mismatched scales of $p\text{CO}_2$ and k estimates
80 (Lauerwald et al., 2015; Raymond et al., 2013) and observations that are generally biased
81 towards larger stream systems (Sawakuchi et al., 2017). Additionally, a recent analysis of global
82 $p\text{CO}_2$ observations suggests that inverse correlations between $p\text{CO}_2$ and k values may result in
83 large overestimations of stream CO_2 fluxes using traditional statistical upscaling methods
84 (Rocher-Ros et al., 2019); however, the effects of this correlation on flux estimates have not been
85 directly tested.

86 While models used to predict fluxes are based primarily on statistical measurements, the
87 processes that control stream CO_2 concentrations and fluxes have been characterized in a number
88 of studies (e.g., Duvert et al., 2018; Horgby et al., 2019a; Horgby et al., 2019b; Hotchkiss et al.,
89 2015; Raymond et al., 2012). Concentrations of CO_2 in streams are determined by the balance of
90 inputs, including soil and groundwater CO_2 and respiration of organic carbon within the water
91 column and hyporheic zone, and outputs such as atmospheric evasion and photosynthesis. In
92 terms of spatial variability of CO_2 concentrations, evasion rates control where on the landscape
93 $p\text{CO}_2$ is highest or lowest, as $p\text{CO}_2$ may degas over scales of 10's of meters (Johnson et al. 2009;
94 Lupon et al., 2019). A number of studies have found that k values which control evasion, are
95 primarily related to discharge and topography, allowing for large-scale estimates based on
96 hydrographic datasets (Raymond et al., 2012; Ulseth et al., 2019). While evasion exerts a strong
97 control on the spatial variability of CO_2 concentrations and fluxes (Rocher-Ros et al., 2019),
98 integrated fluxes from stream networks, however, are controlled primarily by CO_2 sources.

99 Sources of stream CO_2 are broadly categorized as either allochthonous or autochthonous,
100 where allochthonous sources are CO_2 dissolved in soil- and groundwater (GW) that is transported
101 to the stream, and autochthonous CO_2 is produced in the water column or within the hyporheic
102 zone (Marx et al., 2017). While studies have converged on a conceptual model in which
103 autochthonous sources become increasingly important with increasing stream size, the relative
104 balance of these sources remains uncertain. For example, in a survey of USGS NWIS monitoring

105 sites, Hotchkiss et al. (2015) found that while autochthonous contributions increased with stream
106 size, GW was the dominant source across all sites. In contrast, a recent CO₂ budgeting study of
107 1st-3rd order streams in the Cote Du Nord region found that autochthonous sources accounted for
108 ~75% of stream CO₂ (Rasilo et al., 2017). Thus, the lack of constraints on CO₂ source
109 contributions remains a major knowledge gap in terms of our ability to predict stream CO₂.
110 variability.

111 Process-based models that incorporate transport and chemical reactions are extremely
112 useful for disentangling complex natural systems and predicting elemental fluxes (Steeffel et al.,
113 2005). The processes controlling CO₂ in river systems, including where and how they operate,
114 are relatively well-defined; therefore, we are uniquely poised to incorporate these into a
115 predictive model framework. Due to the spatiotemporal variability of *p*CO₂ and complex set of
116 reactions that govern its fate and transport, we argue that a stream network model is an ideal
117 method of mechanistically modeling *p*CO₂ in a manner that allows for *p*CO₂ to be predicted at
118 the high spatial resolution required to accurately calculate landscape fluxes (Rocher-Ros et al.,
119 2019). Beyond predicting *p*CO₂ and fluxes, stream network models can help to determine the
120 relative importance of CO₂ pathways into streams comparing potential contributions of water
121 column and hyporheic zone respiration along with GW CO₂ inputs. Additionally, stream network
122 models can be used to identify potential hotspots and hot moments to guide fieldwork. In this
123 study, we develop and apply a stream network model of stream CO₂ to a mountainous watershed
124 in Gothic, CO containing 1st- 5th order streams. We validate this model against a new high-
125 resolution dataset of stream geochemistry. We further compare model results to existing
126 upscaling and multiple linear regression model techniques, and use the model-data comparisons
127 to evaluate the relative importance of internal and external CO₂ sources.

128 **2 Methods**

129 2.1 Field Site Description

130 This study was conducted in the East River watershed near the Rocky Mountain
131 Biological Laboratory in Gothic, Colorado (USA). The East River watershed delineated at the
132 star shown in Fig. 1 is 87 km² and includes 1st to 5th Strahler order streams. The watershed
133 ranges in elevation from 2,760 to 4,123 m above sea level, has a mean slope of 23° (Winnick et
134 al., 2017), and is broadly representative of watersheds throughout the Rocky Mountains

135 (Battaglin et al., 2011; Markstrom & Hay, 2009). Snow is the dominant form of precipitation in
136 the basin with an average precipitation of $1.23 \pm 0.26 \text{ m y}^{-1}$ and an annual average temperature of
137 1°C (PRISM, 2013). During the sampled period, snow was present in the higher elevations and
138 meltwater was contributing to the discharge (Q). The three major life zones within the basin are
139 alpine, montane, and subalpine (Carroll et al., 2018; Hubbard et al., 2018) and the majority of the
140 watershed is underlain by the Mancos Shale formation in which weathering solute fluxes are
141 dominated by calcium carbonate dissolution and pyrite oxidation (R. W. H. Carroll et al., 2018;
142 Morrison et al., 2012; Winnick et al., 2017). However, the western side of the basin have a
143 greater proportion of Quartz Monzonite Porphyry and tributaries display lower solute
144 concentration when compared to the rest of the watershed (Carroll et al., 2018; Gaskill et al.,
145 1967, 1991).

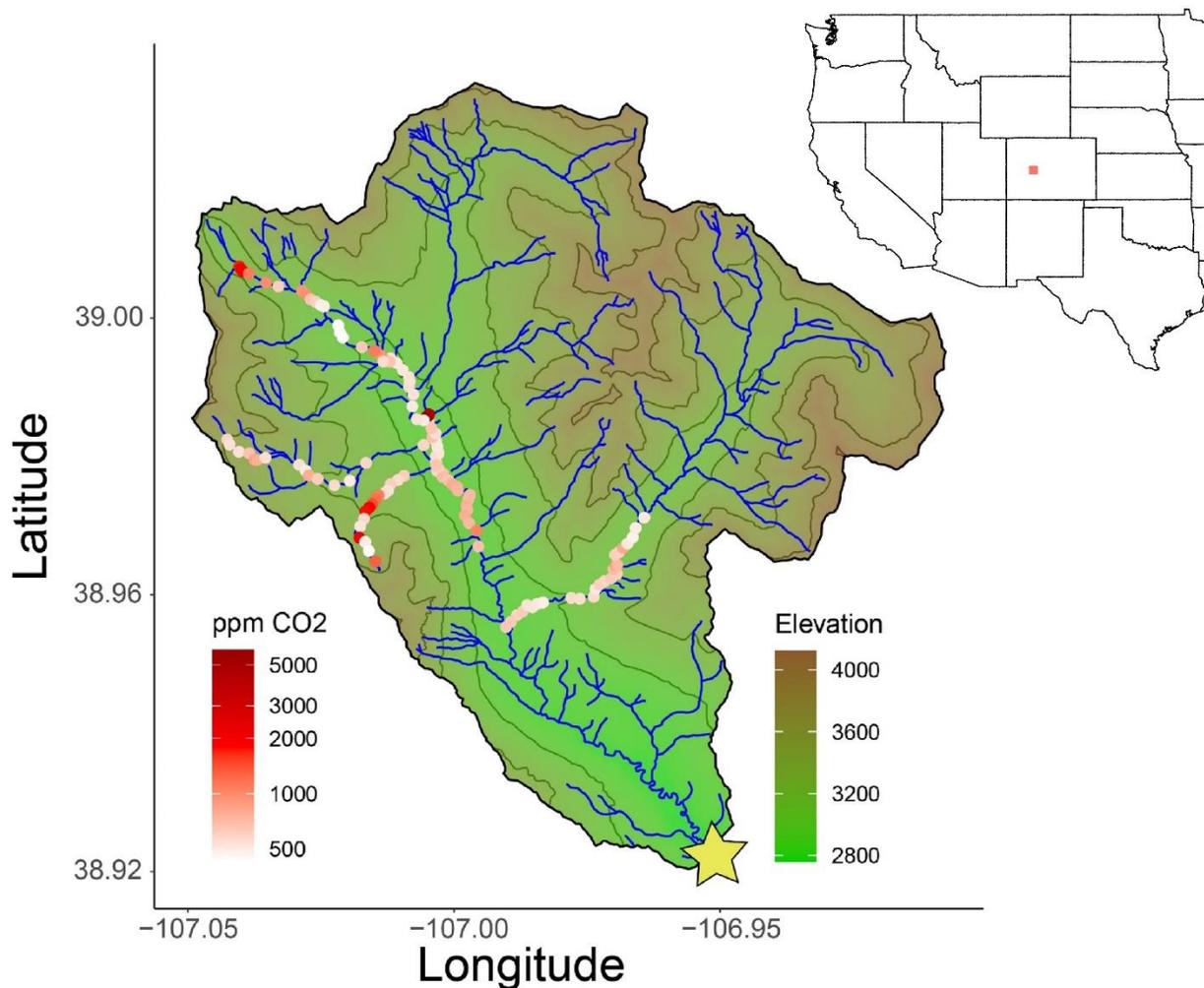


Figure 1: Map of the East River watershed (87 km²) with NHDplus flow lines of the East River and tributaries shown in blue, shaded elevation contours in green, and field-sampled *p*CO₂ (ppm) as points colored from low to high in red (n=121).

147

148 2.2 Sampling Methods

149 Geochemical measurements and stream samples were taken across the East River and its
 150 tributaries over a 10-day period in August 2019 (Fig. 1). While discharge data for this time
 151 period was not available from a proximal gauging station, August discharge values range from
 152 0.43 to 2.81 m³s⁻¹ (2014-2016 and 2018) (star in Figure 1) (Carroll & Williams, 2019) and
 153 precipitation during the sampled days totaled 3.3 cm (Newcomer & Rogers, 2020). Samples were
 154 taken longitudinally along the stream every ~80 m within the designated reaches. At every site,
 155 direct *p*CO₂ measurements were taken using an EGM-5 Portable CO₂ Infra-Red Gas Analyzer
 156 (PP Systems). Samples were prepared by equilibrating 80 ml of stream water with 60 ml of
 157 atmosphere in a gas-tight syringe, which was shaken vigorously for 60 s before direct injection
 158 into the analyzer. Measurements were corrected for atmospheric CO₂ by calculating the total
 159 moles of CO₂ within the sampled air and water at equilibrium then subtracting the moles
 160 estimated in the air at a *p*CO₂ of 400 ppm. Additional measurements such as pH, conductivity,
 161 dissolved oxygen (DO), and temperature were taken with a Yellow Springs Instruments (YSI
 162 Professional Plus) (n=151).

163 2.3 Stream Network CO₂ Model

164 We developed a stream network model based on the advection-reaction equation for
 165 solute transport to predict *p*CO₂ across the East River watershed. These types of models have
 166 been recognized as an important method of estimating elemental fluxes by enhancing the spatial
 167 and temporal coverage of data (Bencala & Walters, 1983). Changes in CO₂(aq) (*C*; mol/L)
 168 through time (*t*) are calculated as,

$$169 \quad \frac{dC}{dt} = -v \frac{dC}{dx} + \frac{1}{A} \frac{dQ}{dx} (C_{gw} - C) - k_{CO_2} (C - C_{atm}) + F_{wc} + F_{he} \quad (1),$$

Table 1: parameters used in the model with “value, Unit” column showing the equation or value used in the model and the “Range” column showing the ranges outputted from the model or the ranges used in the optimization.

Variable	Description	Value, Unit	Range	Data source
C_{atm}	Atmospheric $CO_{2(aq)}$	$2.13e-5, \text{ mol L}^{-1}$	-	
C_{gw}	Groundwater $CO_{2(aq)}$	$0.0012, \text{ mol L}^{-1}$	0.0006-0.0009	optimization
C_{hz}	Hyporheic $CO_{2(aq)}$	$+3.2e-5, \text{ mol L}^{-1}$	$1.1e-5$ - $5.3e-5$	optimization
$C_{wetland}$	Wetland Groundwater $CO_{2(aq)}$	$0.0025, \text{ mol L}^{-1}$	0.0021-0.0027	optimization
DA	Change in area over change in length	m	$3.23e-7$ - $1.05e-4$	DEM
D_m	Molecular diffusion coefficient of CO_2 in water	$1.6e^{-9}, \text{ m}^2 \text{ s}^{-1}$	-	Grant et al., 2018
eD	Energy dispersion rate of the stream	Eq. 4, $\text{m}^2 \text{ s}^{-3}$	0-4.95	Horgby, Segatto, et al., 2019
F	Watershed CO_2 fluxes	Eq. 15, Moles C	-	
F_{he}	Hyporheic zone molar fluxes of $CO_{2(aq)}$	Eq. 8, $\text{mol L}^{-1} \text{ s}^{-1}$	0-0.016	
F_{wc}	Water column molar fluxes of $CO_{2(aq)}$	Sup Eq. X, $\text{mol L}^{-1} \text{ s}^{-1}$	0- $1.8e-5$	
g	Gravitational acceleration	$9.8, \text{ m s}^{-2}$	-	
h	Stream depth	Eq. 13, m	0.03-0.35	Horgby, Segatto, et al., 2019
K_{600}	Gas transfer velocity corrected to 20 °C	Eq.2/3, m d^{-1}	0-0.20	Horgby, Segatto, et al., 2019
K_{CO_2}	Gas transfer velocity of CO_2	Eq. 6, m d^{-1}	0-0.17	Ulseth et al., 2019
k_{hz}	Hyporheic zone gas transfer velocity	Eq. 9, m d^{-1}	0-0.003	Grant et al., 2018
Q	Discharge	$\text{m}^3 \text{ s}^{-1}$	0.01-1.95	
s	Stream slope	*	0-1.81	DEM
sc_t or sc	Schmidt number	Eq. 5/10, *	834.8 or 812	Grant et al., 2018
T	Temperature	$13.7, \text{ }^\circ\text{C}$	-	
u	Shear velocity	Eq. 11, m s^{-1}	0-1.5	Grant et al., 2018
v	Stream velocity	Eq. 12, m s^{-1}	0.01-0.85	Horgby, Segatto, et al., 2019
w	Stream width	Eq. 14, m	0.06-6.62	
x	Distance	m	-	

* unitless

170

171 where v is velocity (m s^{-1}), A is stream cross-sectional area (m^2), Q is discharge ($\text{m}^3 \text{ s}^{-1}$), x is
 172 lateral distance (m), C_{gw} and C_{atm} are the molarity of CO_2 in groundwater and atmosphere-
 173 equilibrated water, respectively (see Table 1 for model variables and descriptions). The molar
 174 fluxes of $CO_{2(aq)}$ ($\text{mol L}^{-1} \text{ s}^{-1}$) from water column and hyporheic zone net respiration are F_{wc} and

175 F_{he} , respectively (Table 1). To estimate potential water column respiration, F_{wc} is set to a
 176 constant rate of $7 \cdot 10^{-11}$ (mol L⁻¹ s⁻¹), which represents the high end of values found by Ward et
 177 al. (2013) in the productive Amazon river as an estimate of maximum potential water column
 178 contributions. The reaeration coefficient of CO₂, k_{CO_2} (s⁻¹), was calculated as the gas transfer
 179 velocity of CO₂ divided by stream depth. The gas transfer velocity of CO₂ was estimated using
 180 k_{600} , based on the equations of Ulseth et al. (2019):

$$181 \quad \ln(k_{600})_{\text{for } eD > 0.02} = 1.18 * \ln(eD) + 6.43 \quad (2), \text{ and}$$

$$182 \quad \ln(k_{600})_{\text{for } eD < 0.02} = 0.35 * \ln(eD) + 3.10 \quad (3).$$

183 Here, eD is the energy dissipation rate of the stream (m² s⁻³) calculated as,

$$184 \quad eD = g * v * s \quad (4),$$

185 where g is the acceleration due to gravity (9.8 m s⁻²), and s is stream slope (unitless, m m⁻¹). In
 186 order to convert k_{600} into k_{CO_2} , we calculated the Schmidt number sc_t (unitless) using the average
 187 daily air temperature T (13.7 °C) of the sampling period and the equation (Wanninkhof, 1992),

$$188 \quad sc_t = 1911 - 118.11 * T + 3.453 * T^2 - 0.0413 * T^3 \quad (5).$$

189 The k_{CO_2} variable was then calculated using the equation (Raymond et al., 2012),

$$190 \quad k_{CO_2} = \frac{k_{600}}{(600/sc_t)^{-0.5}} \quad (6),$$

191 where -0.5 is assumed due to the turbulent surfaces of streams (Jähne et al., 1987; Ulseth et al.,
 192 2019).

193 Equation 1 was solved assuming steady state conditions using a backwards-difference
 194 finite approximation scheme,

$$195 \quad 0 = -v \left(\frac{C_i - C_{i-1}}{\Delta X} \right) + \frac{1}{A} \left(\frac{\Delta Q}{\Delta X} \right) (C_{gw} - C_i) - k_{CO_2} (C_i - C_{atm}) + F_{wc} + k_{hz} * (C_{hz} - C_i) \quad (7),$$

196 with i and $i-1$ representing a grid cell and the previous grid cell respectively. From Eq. 1, F_{he} was
 197 parameterized using the equation,

$$198 \quad F_{he} = k_{hz} (C_{hz} - C) \quad (8),$$

199 where C_{hz} is the molarity of CO_2 in the hyporheic zone and k_{hz} is the hyporheic zone mass
 200 transfer coefficient (m s^{-1}). Using principles of surface renewal theory, k_{hz} was calculated using
 201 the parameterization of Grant et al. (2018) as,

$$202 \quad k_{hz} = 0.17u * sc^{-2/3} \quad (9),$$

203 where u is the shear velocity (m s^{-1}). The assumption that turbulent mixing is the primary process
 204 controlling CO_2 production in the stream bed is supported as the short transit times of the flow
 205 paths caused by turbulent mixing are of similar temporal scale to aerobic respiration (Breugem et
 206 al., 2006; Harvey et al., 2019). Additionally, the lower data requirements of this assumption
 207 allow for the model to be highly scalable. The sc term is calculated as,

$$208 \quad sc = \frac{kv}{D_m} \quad (10),$$

209 where kv is kinematic viscosity of water ($\text{m}^2 \text{s}^{-1}$) and D_m is molecular diffusion coefficient of CO_2
 210 in water ($\text{m}^2 \text{s}^{-1}$). Shear velocity is calculated as,

$$211 \quad u = \sqrt{ghs} \quad (11),$$

212 where s is slope (unitless, m m^{-1}), and h is depth (m).

213 In order to predict $p\text{CO}_2$ across the watershed, we solved Eq.7 for every grid cell
 214 sequentially along each reach starting with 1st order streams. The initial C_i in the first grid cell
 215 within 1st order streams was set to C_{gw} , and C_i values at stream junctions were calculated as the
 216 discharge-weighted mean of all contributing stream model cells. The grid cells were set using
 217 flow line vertices from the NHDplus dataset (U.S. Geological Survey, 2019) which resulted in
 218 variable grid spacing with 392 stream reaches and 7969 model grid cells. Topographic
 219 information for each grid cell such as slope and elevation were retrieved and calculated from a
 220 10m DEM.

221 Due to ongoing snowmelt in the upper basin that lagged snowmelt in the lower basin, we
 222 used elevation to estimate local contributing runoff (m/s) using a linear regression as snow in the
 223 high elevations led to increased Q (Sup Fig. 1) (Carroll & Williams, 2019). The change in
 224 discharge along stream reach ($\Delta Q/\Delta x$ in Eq. 7) was calculated as local runoff multiplied by the
 225 NHDplus reach upstream accumulating area (UAA) per unit length of the stream reach.
 226 Discharge at each grid cell was calculated as the discharge at the previous grid cell plus runoff-

227 based groundwater inputs, assuming constant gaining conditions. The stream width (w), depth
 228 (h), and velocity (v) in meters were calculated using scaling relationships from Horgby et al.
 229 (2019b) for mountainous streams as,

$$230 \quad v = 0.668 * Q^{0.365} \quad (12),$$

$$231 \quad h = 0.298 * Q^{0.222} \quad (13), \text{ and}$$

$$232 \quad w = Q/v/h \quad (14).$$

233 The calculated v along with k_{CO_2} was additionally used to determine stream CO_2 half-life at each
 234 point using a first order reaction,

$$235 \quad \text{half life} = \frac{\ln(2)}{k_{CO_2}/v} \quad (15)$$

236 representing the distance over which stream CO_2 evades assuming no additional CO_2 inputs (Sup
 237 Fig. 2).

238 The model was further amended to capture observed field conditions including wetland
 239 and snow plug locations. Specifically, wetlands are often sources of elevated CO_2 in
 240 groundwater (Buffam et al., 2010; Hope et al., 2004), and snow plugs may act to trap CO_2 in the
 241 stream environment by limiting water-atmosphere interfaces. Snow plugs were defined as large
 242 areas of snow covering the stream, and modeled k_{CO_2} was set to 0 where snow plugs were noted.
 243 Stream sections that were within perennially saturated organic-rich fens were modeled using
 244 $C_{wetland}$ in place of C_{gw} , and field measurements of standing fen pools indicated pCO_2 above the
 245 EGM-5 calibrated range of 25,000 ppm. Lastly, NHDplus headwater flowlines were trimmed to
 246 match points of stream emergence recorded in the field.

247 Within all the above model equations there are only three free parameters: CO_2
 248 concentrations in GW, wetlands, and the hyporheic zone relative to the stream. To tune the
 249 model, we simulated the model across variable ranges of 5000-50000, 10000-100000, and 0-
 250 2000 for C_{GW} , C_{wet} , and $(C_{hz} - C)$, respectively. We chose the optimized values based on
 251 maximum coefficients of determination (R^2) and minimum Root Mean Square Error (RMSE)
 252 from model-data comparisons described below. Model R code along with NHDplus hydrography
 253 datasets for the basin are included in the Supplemental Information.

254 2.4 Statistical Analyses

255 In order to compare the model output to our sampled points, GPS locations of the
256 sampled points were paired with their closest model grid cell. The paired points were filtered to
257 remove any that were more than 50m apart, or for which there was no NHDplus counterpart
258 (n=30). Points without NHDplus counterparts comprised seeps and small streams that were not
259 represented by NHDplus flowlines. The remaining 121 points of which 12, 23, 21, and 65 are 1st
260 – 4th order respectively, were compared using model-data R^2 , RMSE, and t-tests to the stream
261 network model with and without benthic respiration (BZ) to determine if the addition of internal
262 processes add predictive power to the model. All calculations were conducted using R (R Core
263 Team, 2020; Supplemental Information).

264 A multiple linear regression model (MLRM) predicting pCO_2 based on Q , velocity,
265 slope, elevation, and mean watershed net primary production (NPP) (NASA, 2019) was
266 determined using a stepwise approach. Using Q , k_{CO_2} , velocity, slope, elevation, stream order,
267 k_{hz} , mean watershed NPP, and landcover as the initial inputs, all possible regression
268 combinations were calculated. The best regression model was chosen based on the lowest AIC
269 value that contained only significant predictors ($p < 0.05$). The final regression was evaluated by
270 calculating the mean and variance of the pCO_2 predicted as well as comparing the R^2 and RMSE
271 values. Additionally, global scale mountainous inland water CO_2 fluxes were recently estimated
272 using an MLRM based on pCO_2 data in the European Alps (Horgby et al., 2019b). The
273 regression consisted of elevation, Q , and soil organic carbon (SOC) from Hengl et al. (2017). For
274 comparison, we applied this model to the East River watershed to test the potential scalability of
275 the Horgby MLRM to different field areas.

276 Additionally, we compared existing statistical upscaling methods for estimating
277 watershed-scale CO_2 fluxes based on point measurements to integrated model output. Two
278 common methods of upscaling CO_2 evasion fluxes were evaluated against the stream-network
279 modeled fluxes. The flux estimation methods evaluated used Eq. 16 and the same k_{CO_2} , h , w , and
280 Δx as the stream network model. In the upscaling models, pCO_2 was calculated as 1) mean pCO_2
281 from all samples across the watershed; and 2) mean stream pCO_2 by Strahler order (Butman &
282 Raymond, 2011; Raymond et al., 2013). The corresponding CO_2 fluxes were compared to stream
283 network model fluxes for each stream order. The watershed-scale CO_2 evasion fluxes (F) were
284 calculated for the modeled and regression data using the equation,

$$F = \sum(C_i - C_{atm}) * k_{CO_2} * h * w * \Delta x \quad (16).$$

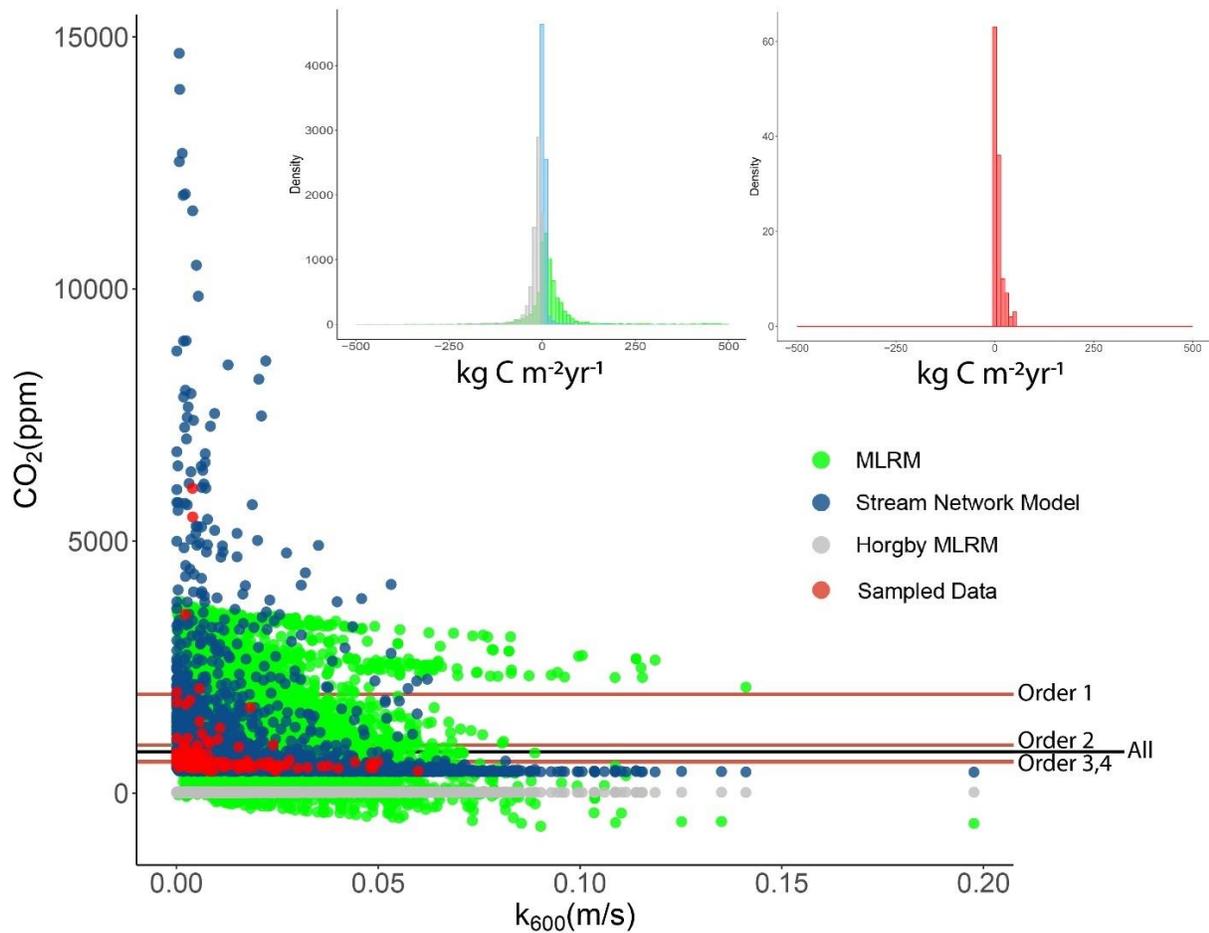
286 Additionally, we repeated the upscaling methods with flux estimates restricted to the reaches
287 with sampled data to evaluate model and upscaling performance within well-characterized areas.

288 **3 Results**

289 3.1 Observational Data

290 Stream waters across the East River and its tributaries had a mean temperature of 8.1 °C
291 ranging from 2.7 – 14 °C at elevations ranging from 2873 – 3521 m. Across all sample points,
292 the mean dissolved oxygen (DO) was 91% and ranged from 0.4 – 11.4 mg L⁻¹. The mean pH was
293 8.03 ranging from 7.14 – 8.4. Roughly 90% of samples were below 8.3, such that bicarbonate
294 was the dominant inorganic carbon species present. Conductivity within the data ranged from
295 11.6 – 263.1 μs cm⁻¹ with a mean of 112.4 μs cm⁻¹.

296 Measured *p*CO₂ was consistently elevated above atmospheric concentrations with a mean
297 of 820 ppm and range of 433-6044 ppm (Fig. 1). First order streams had the highest mean *p*CO₂
298 at 1963 ppm. Increasing stream order generally corresponded to decreasing mean *p*CO₂, with
299 2nd-4th order streams having mean *p*CO₂'s of 952, 616, and 628 ppm respectively. The minimum
300 *p*CO₂ within each order showed little variation, ranging from 433-527 with no correlation to
301 stream order; however, the maximum values decreased with increasing stream order with a *p*CO₂
302 of 6044, 2074, 1090, and 1040 ppm in 1st – 4th order streams respectively. Additionally, *k*_{CO₂} was
303 found to restrict in-stream *p*CO₂ as 95% of sampled points with *k*_{CO₂} values of greater than 0.005
304 (m/s) had *p*CO₂<1000, similar to findings in a Swedish catchment system (Fig. 2) (Rocher-Ros
305 et al., 2019).



306

Figure 2: Stream $p\text{CO}_2$ plotted against k_{600} in m/s with MLRM in green, stream network model in blue, Horgby MLRM in gray, and sampled data in red. Lines show values used in the upscaling calculations with brown lines representing mean $p\text{CO}_2$ in 1st – 4th order streams top to bottom and the black line is the mean of all sampled $p\text{CO}_2$. Histogram of fluxes are shown in the inset with sampled data shown separately so variability can be seen.

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Point sample data was used to estimate total watershed CO_2 fluxes based on two separate upscaling methods as described above (Butman & Raymond, 2011; Raymond et al., 2013). The first method used the mean sampled $p\text{CO}_2$ and applied it across the entire stream model using the modeled stream morphology and k_{CO_2} , which resulted in total watershed fluxes of $6.4 \pm 11.6 \text{ Gg C yr}^{-1}$ (Raymond et al., 2013). The second method was to predict CO_2 fluxes separately for each stream order using the mean $p\text{CO}_2$ within each order as the order's CO_2 concentration while maintaining the other modeled parameters. This predicted $p\text{CO}_2$ fluxes of $6.3 \pm 5.8 \text{ Gg C yr}^{-1}$ with

315 1st-5th orders contributing 2.7 ± 3.5 , 0.9 ± 0.8 , 0.4 ± 0.4 , 0.8 ± 0.4 , and 1.5 ± 0.8 Gg C yr⁻¹, respectively.
 316 Additionally, flux predictions were restricted to the 2508 m of sampled reaches out of the total
 317 164872 m in the east river. This was done in order to compare upscaling methods to sampled
 318 data on a one-to-one basis (Table 2). This resulted in a prediction of 0.06 Gg C yr⁻¹ released from
 319 the sampled reaches based on measured data, 0.15 Gg C yr⁻¹ based on mean $p\text{CO}_2$, and 0.09 Gg
 320 C yr⁻¹ based on mean $p\text{CO}_2$ by order showing that the signal mean method predicted fluxes 2.5x
 321 more than sampled data and the mean by order method predicted 1.5x the fluxes of sampled data.

Table 2: model performance with RMSE and R^2 for the full data range and R^2 by order. Predicted range of $p\text{CO}_2$ and CO_2 flux are shown for each model for the entire watershed and only within the sampled reaches.

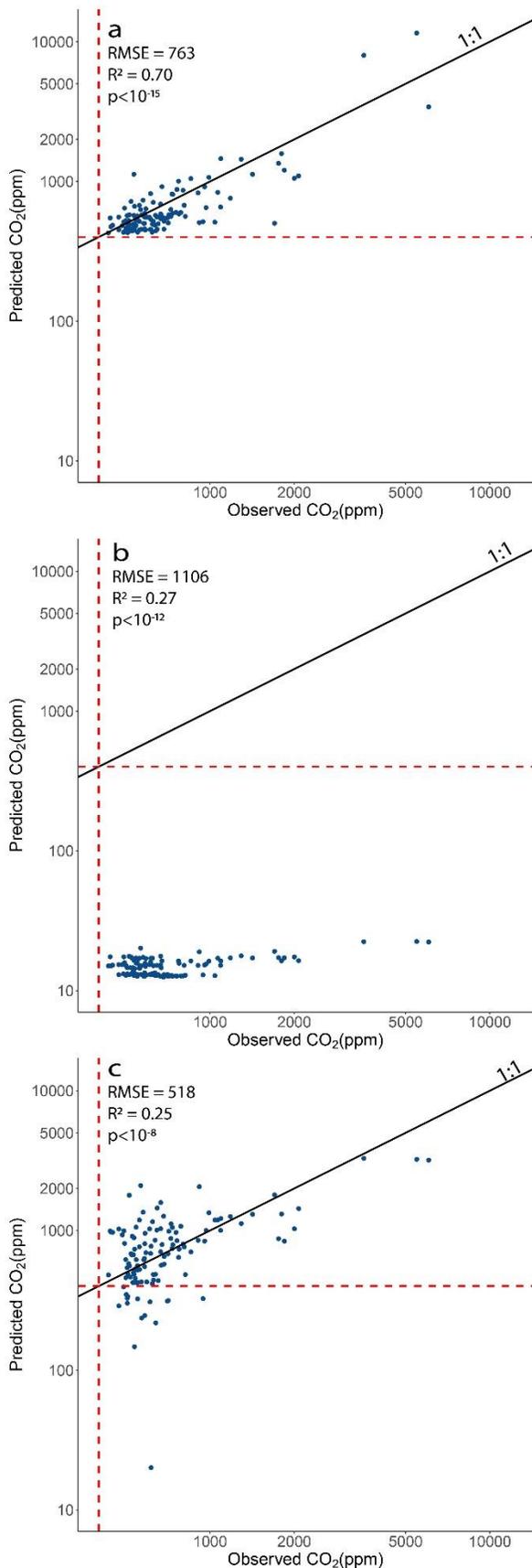
	$p\text{CO}_2$ range(ppm)	R^2	P	RMSE	R^2 1 st order	R^2 2 nd order	R^2 3 rd order	R^2 4 th order	Fluxes Gg C/yr	Sampled reach Fluxes Gg C/yr
Sampled data	433 - 6044	-	-	-	-	-	-	-	-	0.06
Stream network Model	416 - 18000	$0.7 < 10^{-15}$		763	0.71	0.57	0.49	0.34	1.3	0.03
MLRM	-660 - 3804	$0.25 < 10^{-8}$		518	0.75	0.03	0.01	0.17	17.7	-
Horgby MLRM	12 - 32	$0.27 < 10^{-12}$		1106	0.79	0.03	0	0.02	-5.9	-0.14
Upscaling by Mean $p\text{CO}_2$	820	-	-	-	-	-	-	-	6.4	0.15
Upscaling by Mean order $p\text{CO}_2$	628 - 1963	-	-	-	-	-	-	-	6.3	0.09

322

323 3.2 Model Results

324 The optimization of the model resulted in a $C_{GW} p\text{CO}_2$ of 18,000 ppm, $C_{wet} p\text{CO}_2$ of
 325 44,000 ppm, and a hyporheic zone $p\text{CO}_2$ elevation ($C_{hz} - C$) of 600 ppm. The best three
 326 optimizations runs all had the same C_{GW} value, which falls within the range of sub-soil (>30 cm)
 327 growing season $p\text{CO}_2$ values measured in a soil profile within the East River (~7,000 – 23,000
 328 ppm; Winnick et al., 2020). Wetland $p\text{CO}_2$ measured in the East River was above the 25,000
 329 ppm calibration of the EGM-5 supporting the elevated model optimization value. The hyporheic
 330 zone $p\text{CO}_2$ was found to be elevated above stream $p\text{CO}_2$ by 600 ppm which was at the upper
 331 range (~0 – 700 ppm) (Sup Fig. 3) of values calculated from measured pH and estimated
 332 alkalinity (Nelson et al., 2019).

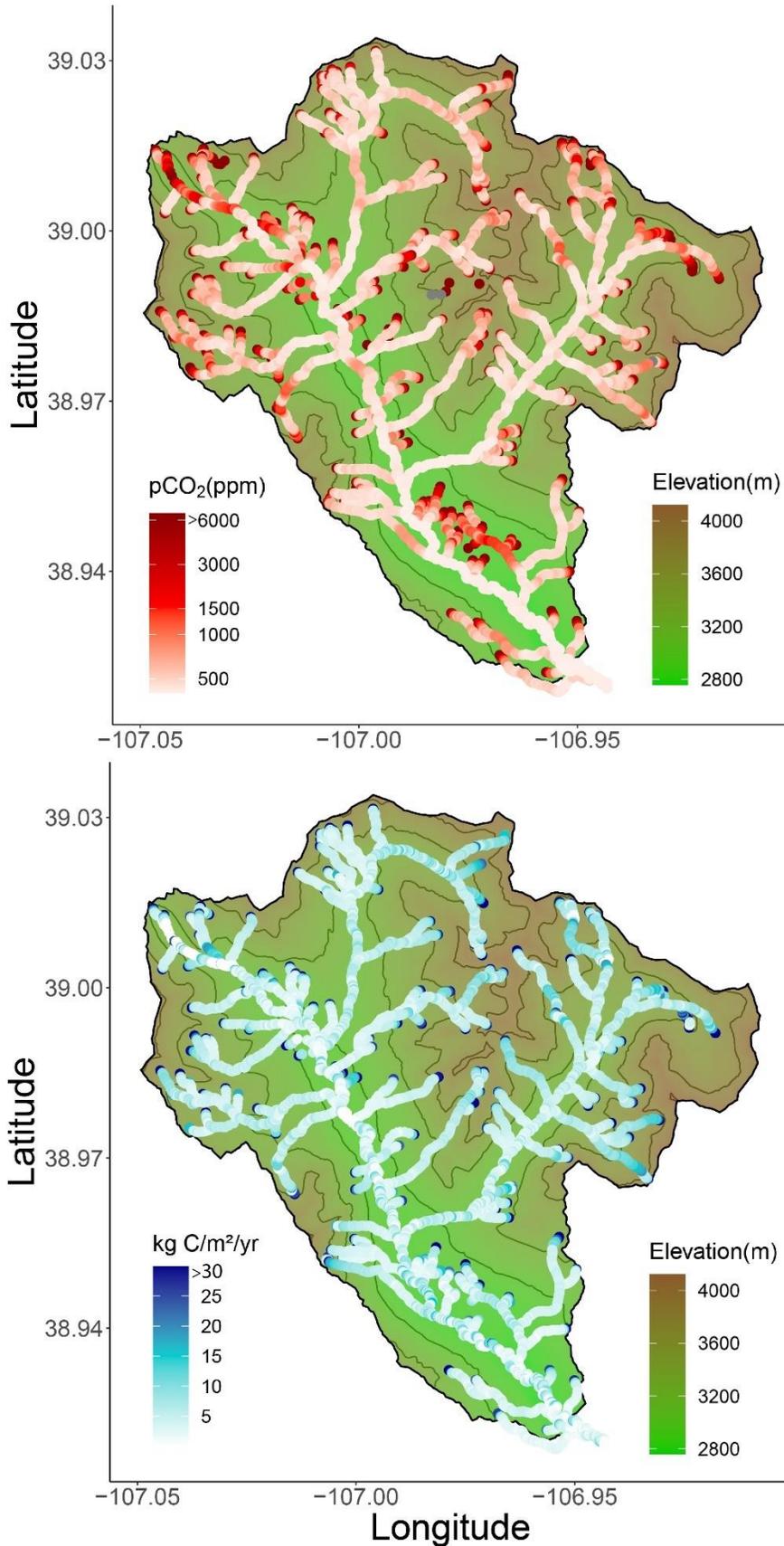
333 The full model predicted $p\text{CO}_2$ values and captured observed spatial patterns with a
 334 RMSE of 763 ppm, R^2 of 0.70 ($p < 10^{-15}$) for $\ln(p\text{CO}_2)$, and a paired t-value of 0.30 (df=120,
 335 $p=0.76$) for $p\text{CO}_2$ when compared to observed data (Fig. 3). The GW-only stream network model



had an RMSE of 1008 ppm, and R^2 of 0.69 ($p < 10^{-15}$) for $\ln(p\text{CO}_2)$, and paired t-value of 0.34 ($df=120$, $p=0.74$) for $p\text{CO}_2$. The paired t-test suggests a mean underestimation of 31 ppm between matched points for the GW-only model and 21 ppm for the full model with neither model showing significant difference ($p > 0.05$) from the observed $p\text{CO}_2$ values. As the Full model outperformed the GW-only model in all three metrics of validity, from this point on we

Figure 3: Model-data comparisons and statistics for the (a) stream network model; (b) Horgby MLRM; and (c) MLRM with 2 points missing as they were negative. The dashed lines (red) represent atmospheric will refer to the full model.

Stream network model $p\text{CO}_2$ was consistently elevated above atmospheric concentrations ranging from 416 ppm to optimized GW values with a mean of 1087 ppm, compared to the measured range of 433-6044 ppm (Fig. 4). The largest discrepancy between the model and the sampled data were at highest observed $p\text{CO}_2$ locations; however, 95% of modeled points were within 400 ppm above and 950 ppm below the sampled points. The highest $p\text{CO}_2$ values were predicted in the headwaters at points of spring emergence and quickly approached atmospheric values. Across all model points, the median calculated CO_2 half-



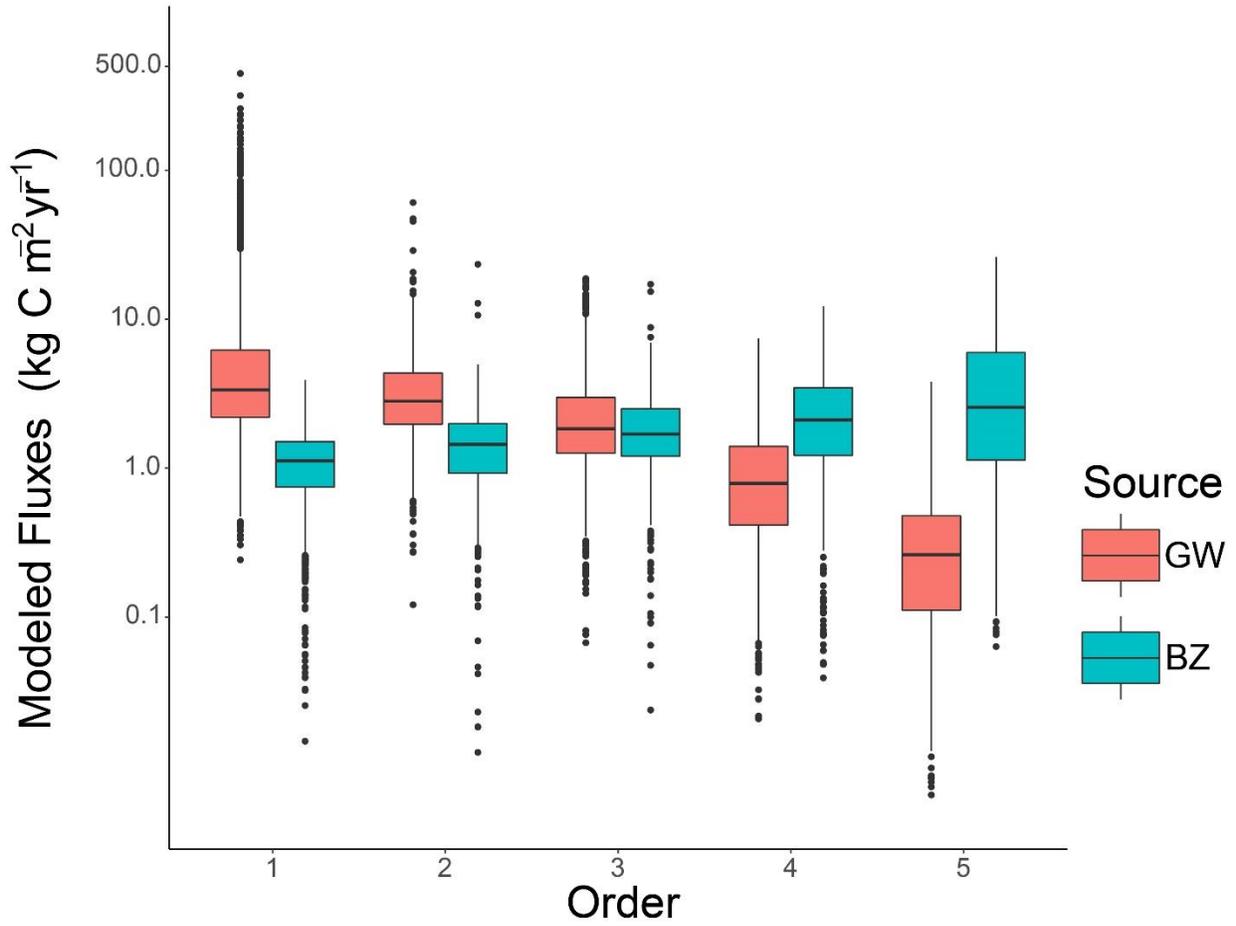
life was 11 m. As a result, model $p\text{CO}_2$ was strongly restricted by k_{CO_2} ; 95% of sampled points with k_{CO_2} values of

Figure 4: (A) Stream network modeled $p\text{CO}_2$ in the East River shown in red; (B) Stream network model area-normalized CO_2 fluxes shown in blue with fluxes $>30 \text{ kg C/m}^2/\text{yr}$ shown in black ($\sim 1\%$ of stream at locations of stream emergence only) greater than $\sim 0.005 \text{ (s}^{-1}\text{)}$ had $p\text{CO}_2 < 1000 \text{ ppm}$ (Fig. 2).

Modeled patterns were similar to observational data with mean $p\text{CO}_2$ decreasing as stream order increased: 1st-5th order streams had a mean $p\text{CO}_2$ of 1835, 704, 578, 524, and 468, respectively. Similarly, the max $p\text{CO}_2$ showed a decreasing pattern with stream order with 1st-5th orders having 18000,

382 8767, 2612, 879, and 535 ppm, respectively. The minimum $p\text{CO}_2$ showed no pattern across
383 orders with 1st -5th order streams having 430, 416, 421, 419, and 419 ppm respectively.

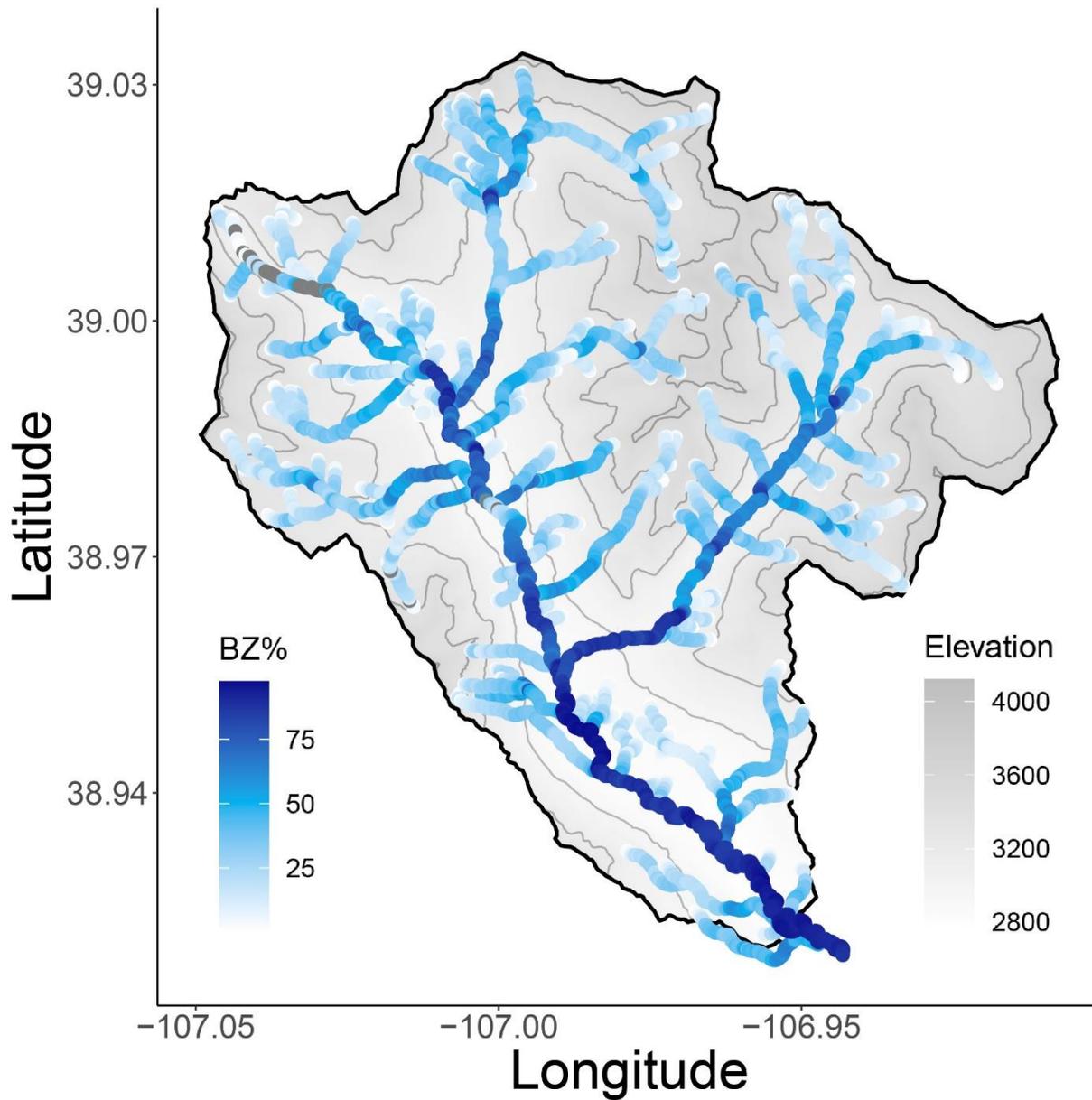
384 The full stream network model predicted a mean flux of $6.3 \text{ kg C m}^{-2} \text{ yr}^{-1}$ ranging from 0
385 - $448 \text{ kg C m}^{-2} \text{ yr}^{-1}$ with total watershed fluxes at 1.3 Gg C yr^{-1} (Fig.4, Table. 2). The highest
386 fluxes were predicted in first order reaches totaling 0.4 Gg C yr^{-1} with mean area-normalized
387 fluxes of $9.3 \text{ kg C m}^{-2} \text{ yr}^{-1}$. Total fluxes showed a decrease with order until the 3rd order, at which
388 point fluxes increased with order releasing 0.44, 0.20, 0.19, 0.22, and 0.26 Gg C yr^{-1} in 1st-5th
389 order stream respectively. The stream network model suggests that GW is the largest source of
390 CO_2 in river systems accounting for 53% of CO_2 emitted, followed by benthic respiration at
391 47%, and water column respiration at 0.1% (Fig. 5). Absolute GW fluxes show a weak negative
392 correlation with Q ($R=-0.1$) whereas benthic respiration showed a strong positive correlation
393 ($R=0.47$) with Q. In first order streams, GW contributed 86% of the C fluxes whereas benthic
394 respiration contributed 14%. In the fourth and fifth order streams benthic respiration was 72%
395 and 91% of the fluxes compared to the 28% and 8% contributed by GW (Fig. 6). We note that
396 while precise percent contributions are highly dependent on optimized C_{HZ} values, this overall
397 pattern is a robust feature of the stream network model matching conceptual models of stream
398 CO_2 sources.



401

Figure 5: Area-normalized model fluxes from first through fifth order streams with red (left) box representing groundwater contributions and blue (right) representing benthic zone respiration contributions of CO₂. 86 points not shown <0.005.

402



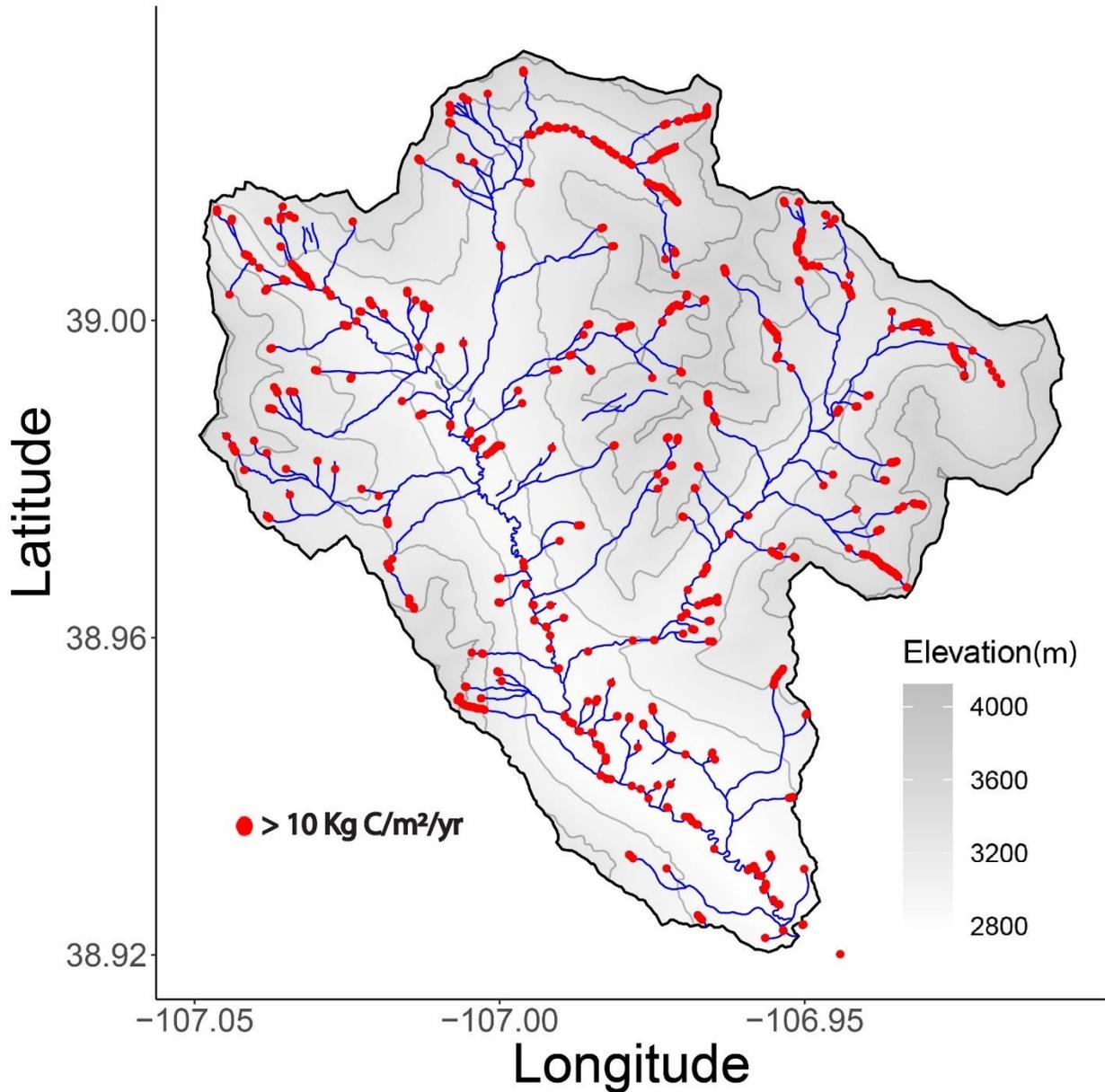
405

Figure 6: Modeled % benthic zone (BZ) respiration CO₂ contributions at each stream location.

406

407 The model suggests that 11% of the East River by length has a CO₂ flux greater than 10
 408 kg C m⁻² yr⁻¹ (Fig. 7), with 78% of these hotspots in 1st order streams and only 4% in 5th order
 409 streams. However, as headwaters are a disproportionate length of the stream, we compared the %
 410 hotspots within each order to the total stream length of that order. We found that 1st orders are
 411 17% hotspots and that 5th order streams had the second largest proportion of hotspots at 9% with
 412 2nd, 3rd, and 4th having 4%, 6%, and 4% respectively. Hotspots throughout the East River and

415 within each order had significantly higher slope than the mean of the total network or of the
 416 respective order. Groundwater dominated hotspots in 1st – 3rd order streams with the BZ
 417 contributing 7%, 20%, and 16% respectively whereas BZ respiration was a greater % of CO₂
 418 fluxes in 4th and 5th order streams at 74% and 93% respectively (Sup Table. 1).



419

Figure 7: Map of modeled CO₂ flux hotspots. Stream points with area-normalized fluxes greater than 10 kg C m⁻² yr⁻¹ are shown in colored points with streamlines shown in blue.

420

421 The stream network model outperformed the stepwise MLRM which found Q , velocity,
 422 slope, elevation, and mean watershed NPP to be the only significant predictors of $p\text{CO}_2$ (C_{MLRM}),
 423 hence referred to as the MLRM. The MLRM

$$424 C_{MLRM} = 3599.479 * Q - 8726.124 * v - 1226.308 * s - 3.409 * e - 4.184 * NPP +$$

$$425 14817.114 \quad (17).$$

426 predicted $\ln(p\text{CO}_2)$ with a R^2 of 0.25 ($p < 10^{-8}$) and a RMSE of 518 (Fig. 3). The RMSE of the
 427 MLRM is better than the stream network model as the MLRM preferentially fits the higher $p\text{CO}_2$
 428 values; however, the low R^2 shows that it is worse at predicting $p\text{CO}_2$ variability, particularly
 429 below ~ 1500 ppm, to the point that negative values are predicted within 2.6% of the East River.
 430 Alternatively, the higher RMSE of the stream network model is due to the difficulty in fitting the
 431 higher $p\text{CO}_2$ values which is likely due to sensitivity of stream emergence location and spring
 432 velocities. Additionally, the MLRM predicted a smaller range of $p\text{CO}_2$ -660 – 3804 ppm than the
 433 observed data and stream network model. Using the MLRM across the east river watershed
 434 resulted in an estimated CO_2 flux of $17.7 \text{ Gg C yr}^{-1}$ ($18.3 \text{ Gg C yr}^{-1}$ when excluding negatives)
 435 with a mean area normalized flux of $38.5 \text{ kg C m}^{-2} \text{ yr}^{-1}$ (Table 2).

436 The MLRM used in Horgby et al. (2019b), hence referred to as the Horgby MLRM, was
 437 compared to observations and showed less accuracy when predicting $\ln(p\text{CO}_2)$ with an R^2 of
 438 0.27 $p < 10^{-12}$ RMSE of 1106 (Fig. 3), below the $R^2=0.39$ $p < 0.001$ presented in the original paper.
 439 Importantly, the Horgby MLRM predicts sub-atmospheric $p\text{CO}_2$ values across the watershed in
 440 direct contrast with observations. When used to calculate fluxes, this method therefore predicts
 441 the East River to be a CO_2 sink, sequestering 5.9 Gg C yr^{-1} (Table 2) with an area-normalized
 442 mean of $17.7 \text{ kg C m}^{-2} \text{ yr}^{-1}$, which is within the $0 - 27 \text{ kg C m}^{-2} \text{ yr}^{-1}$ predicted to be sequestered in
 443 the region in the original paper. Additional disadvantages of these linear regression models are
 444 that the soil organic carbon map is at coarser resolutions (250 m^2) (Hengl et al., 2017) than
 445 available DEMs.

446 **4 Discussion**

447 4.1 Stream network models versus statistical predictions of $p\text{CO}_2$

448 To the best of our knowledge this paper represents the first stream network model to
 449 predict $p\text{CO}_2$, although the methodology is similar to previous nitrogen stream network models
 450 (Gomez-Velez et al., 2015; Gomez-Velez & Harvey, 2014). Here we show that using a high-

451 resolution 10m DEM and estimated groundwater $p\text{CO}_2$, we are able to predict stream $p\text{CO}_2$ at
452 sub-100 m (22 m mean distance between points) resolution across NHDplus flowlines. Notably,
453 the model is able to capture structural characteristics of stream CO_2 observations that emerge
454 naturally from the representation of physical processes. These include (1) GW CO_2 hotspots
455 based on spring emergence and topographic convergence, in which stream CO_2 decays over
456 spatial scales of $\sim 10^1\text{--}10^2$ m depending on the balance of advection and gas exchange (Fig. 4);
457 (2) diminishing influence of GW inputs with increasing stream size (Fig. 6); (3) atmosphere-
458 super-saturated CO_2 in higher-order streams from stream corridor CO_2 production (Fig.'s 4,6);
459 and (4) inverse correlations between gas exchange velocities and $p\text{CO}_2$ (Fig. 2).

460 This ability to capture the qualitative structure of spatial variability is borne out by
461 significantly stronger model-data correlations for the stream network model ($R^2=0.70$) versus the
462 MLRM ($R^2=0.25$) and Horgby MLRM ($R^2=0.27$). This structural advantage is even more
463 pronounced when comparing model-data correlation within Strahler stream order. The stream
464 network model predicted $\ln(p\text{CO}_2)$ in 1st-4th order streams with a R^2 of 0.71*, 0.57*, 0.49*, and
465 0.34* respectively compared to the MLRM's R^2 of 0.75*, 0.03, 0.01, and 0.13* in first to fourth
466 order streams, asterisk denote significance (Table 2). This shows that the stream network model
467 has an improved ability to predict $p\text{CO}_2$ especially within higher order streams as it has
468 improved resolution at lower concentrations. While the MLRM features better RMSE values
469 compared to the stream network model, this is due to the bias of linear regression models to
470 capture extreme values associated with spring emergence as demonstrated by the high model-
471 data R^2 value for 1st order streams. Additionally, the MLRM did not correlate with data from 2nd
472 and 3rd order stream further showing its inability to accurately predict CO_2 at lower
473 concentrations, to the point that negative values are predicted across 2.6% of the East River.

474 One of the primary reasons MLRM's are unable to capture the structure of stream CO_2
475 variability across and within stream orders is the implicit treatment of each stream location $p\text{CO}_2$
476 as independent. In reality, $p\text{CO}_2$ at any given location within the stream network represents a
477 combination of local processes and upstream history. Additionally, the inability of MLRM's to
478 capture realistic patterns outside of training datasets (negative $p\text{CO}_2$ values from the MLRM and
479 sub-atmospheric $p\text{CO}_2$ from the Horgby MLRM) suggests that empirical relationships between
480 landscape variables and local $p\text{CO}_2$ involve a large degree of non-stationarity, limiting their

481 potential transferability or scaling potential. This can be seen in the MLRM as negative values
482 were most common in 1st – 3rd order streams with 30%, 18%, and 48% of negative predictions
483 respectively, and all negative values were predicted above an elevation of 2958 m. The Horgby
484 MLRM is strongly dependent on elevation, with sub-atmospheric values predicted above ~3000
485 m in the original paper (Horgby et al., 2019b). We suggest that this may relate to vegetation in
486 the European Alps versus the Colorado Rockies, in which a lack of high elevation organic matter
487 may limit allochthonous CO₂ sources in the Alps.

488 As the stream network model represents physical processes, it has the potential to be
489 highly transferable across sites, which will be tested in future research. Notably, data
490 requirements for the stream network model are roughly equivalent to MLRM's and existing
491 estimation methods of gas transfer velocities (e.g., Raymond et al., 2012; Ulseth et al., 2019). In
492 this application, we used stream data observations to optimize free parameters including GW,
493 wetland, and hyporheic zone $p\text{CO}_2$; however, the model may be supplemented in future studies
494 with site-specific measurements of these quantities or empirical models to estimate how these
495 parameters vary across environments. Overall, we argue that the stream network model
496 framework represents a significant improvement over existing empirical methods for estimating
497 stream $p\text{CO}_2$.

498 4.2 Implications for global stream CO₂ fluxes

499 The improved resolution and $p\text{CO}_2$ estimation of the stream network model allow for a
500 more robust estimation of CO₂ fluxes from the East River. Upscaling methods predicted CO₂
501 fluxes to be ~5x larger than the stream network model. The elevated predictions from statistical
502 upscaling methods likely stem from an overestimation of $p\text{CO}_2$ in reaches with high k_{CO_2} as the
503 estimated CO₂ concentrations are likely higher than would be expected at these locations (Fig. 2).
504 Additionally, the structure of $p\text{CO}_2$ data lends itself to further overestimation as it commonly is
505 right-skewed with few large CO₂ concentrations causing the mean and median to be larger than
506 the mode (Sup Fig. 4). As described above, the Horgby MLRM estimates the East River as a CO₂
507 sink, which suggests their estimates of global mountainous stream CO₂ fluxes may be artificially
508 low. The MLRM predicted a CO₂ flux 13x greater than the stream network model even though
509 13% of the model was predicted to be a CO₂ sink, this is likely due to the prediction of $p\text{CO}_2$
510 values in the 2000s at relatively high $k_{600} > 0.06$ m/s (Fig. 2) as hypothesized by Rocher-Ros et

511 al. (2019). The overestimation of CO₂ fluxes seen here confirm that spatial mismatches between
512 model variables represent an important issue in current stream CO₂ emission estimates.

513 Taken together, these analyses support the idea that current global budgets may
514 significantly overestimate CO₂ fluxes from rivers and streams. While site-based discrepancies
515 between upscaling and MLRM versus stream network fluxes are high (500-1300%), we note that
516 these discrepancies are likely maximized due to the mountainous terrain and elevated gas
517 exchange velocities. Future work will target the impact of *k-p*CO₂ inverse correlations in
518 lowland environments and at regional to global scales. Notably, this may result in a significant
519 downward revision in global stream CO₂ estimates, as has recently been suggested (Rocher-Ros
520 et al., 2019).

521 4.3 Internal production vs external inputs

522 The proportion of external and internal sources of CO₂ fluxes in streams is an active area
523 of research, as relative contributions from GW, the soil zone, water column respiration, and the
524 hyporheic zone remain uncertain. Quantifying internal and external sources of CO₂ is difficult
525 and requires extensive field experiments to create C budgets for individual reaches (e.g. Rasilo et
526 al., 2017). This has reduced our broader understanding of CO₂ sources as these field and data
527 intensive studies do not sufficiently cover the range of stream orders, discharges, or landscape
528 characteristics that control the processes contributing to stream CO₂. However, using the full
529 stream network model, we are able to estimate the proportions of CO₂ from internal and external
530 sources that are consistent with field observations from the East River and larger-scale data
531 compilations.

532 As described above, the model predicts diminishing influence of GW inputs with
533 increasing stream size, consistent with previous studies (Hotchkiss et al., 2015). Additionally, the
534 stream network model suggests that water-column respiration contributes minimally to stream
535 network CO₂ fluxes. This result occurs despite the use of relatively high water-column
536 respiration rates throughout the watershed, and is consistent with the budget analysis of Rasilo et
537 al. (2017) for 1st-3rd order streams in the Cote du Nord region. We note that water-column
538 respiration likely becomes increasingly important at larger stream sizes as has been noted for
539 N₂O production (Marzadri et al., 2017).

540 Our stream network model further suggests that hyporheic zone respiration within stream
541 benthic layers is the primary source of CO₂ in 4th and 5th order streams, consistent with Rasilo et
542 al. (2017) and contrasting with Hotchkiss et al. (2015). We note that model-data statistical
543 agreement is relatively insensitive to the precise value of hyporheic zone *p*CO₂ used, which itself
544 is likely highly variable across the East River; however, our optimized value agrees well with
545 previously published benthic zone pore water geochemistry from the main stem of the East River
546 (Nelson et al., 2019; Supplementary Information). Despite its potential role in controlling higher-
547 order stream CO₂ concentrations and fluxes, very few studies have sought to characterize the
548 dynamics hyporheic zone carbon production, which instead have focused primarily on nitrogen
549 and oxygen dynamics. Thus, an improved understanding of hyporheic zone CO₂ production and
550 exchange is strongly needed to accurately estimate stream CO₂ concentrations and fluxes.

551 Although overarching patterns of decreasing external contributions with order hold across
552 the range of modeled HZ *p*CO₂, a mosaic of BZ and GW dominated sections exist within mid
553 order stream showing that small scale variability plays an important role. This can be seen most
554 readily within 3rd order streams where 60% of the stream length is GW-dominated (Fig. 5,6). In
555 2nd and 4th order streams we see less extreme patchiness with 85% and 6% of streams by length
556 GW dominated respectively. This emphasizes that local conditions may deviate from predicted
557 patterns, as these transitions within stream systems represent a patchwork dynamic rather than a
558 smooth gradient.

559 4.4 Hotspots

560 The magnitude and spatial distribution of carbon fluxes has been the focus of many
561 studies, which have found headwaters to be hotspots of CO₂ fluxes, defined here as locations
562 with CO₂ fluxes greater than 10 kg C m⁻² yr⁻¹. More recent studies have begun to characterize the
563 interplay of topographically driven evasion and sources of CO₂ which create a mosaic of fluxes
564 and hotspots through stream systems (Duvert et al., 2018; Rocher-Ros et al., 2019). In the past,
565 upscaling and coarse resolution MLRM's have hindered our ability to parse out where in
566 landscapes these hotspots are. Using the stream network model, we are able to predict where in
567 the landscape these hotspots are and their relative contribution to integrated fluxes across stream
568 orders. From this we can see that first order streams are the largest contributors making up 78%
569 of the East Rivers hotspots (Fig.7) agreeing with findings from Duvert et al. (2018) which shows

570 that headwaters are hotspots of CO₂ evasion. However, 5th order streams feature higher
571 proportional hotspot areas as compared to 2nd-4th order streams, making 5th order streams a
572 potentially important source of CO₂ fluxes. Although 5th order streams may have more hotspots
573 then previously surmised, they are still of a smaller magnitude than 1st order streams as the total
574 fluxes were still greater in 1st order streams.

575 Hotspots in the East River were more likely to be in GW dominated sections, with 93%
576 of hotspots by length receiving greater than 50% of their CO₂ from GW. Comparatively, only
577 75% of the East River length was GW-dominated. This pattern of GW-supplied hotspots held in
578 1st – 3rd order streams but inverted in 4th and 5th order streams where hotspots were more likely to
579 be in locations where CO₂ was dominantly supplied by BZ respiration. The location of this
580 inversion has additional significance as 3rd - 4th order streams are where the switch from GW to
581 BZ dominated inputs occurs, showing that hotspots are not purely groundwater supplied but
582 instead can be supplied through internally produced *p*CO₂. Additionally, the mean slope of
583 hotspots is steeper than the mean stream slope of the East River showing that hotspots likely
584 occur in areas of transition from low to high slopes where CO₂ that has built up in low slope
585 reaches is quickly lost when *k* increases, similar to previous findings (Rocher-Ros et al., 2019).
586 As stream network models are able to predict hotspots and parse out CO₂ sources and
587 topographic controls in actual stream environments, they may further provide the ability to guide
588 target field sampling.

589 **5 Conclusions**

590 Predicting regional and global stream CO₂ emissions remains challenging, and estimates
591 continue to change due to additional sources of data and methodological improvements (Drake et
592 al., 2018). Many of these improvements have additional sources of error including mismatches
593 between data resolution which can become a significant when upscaling (Rocher-Ros et al.,
594 2019). Here, we tested the ability of a stream network model to improve predictions of stream
595 CO₂ concentrations and fluxes through representation of physical hydrologic processes,
596 including atmospheric gas exchange, downstream advection, groundwater inputs of CO₂, and
597 benthic respiration driven by turbulent mixing. These process-based predictions outperform
598 statistical methods within the East River, and future work will test the accuracy of the stream
599 network model when applied to other systems. The stream network model also provides direct

600 estimates of the proportion of external and internal CO₂ contributions. The model suggests that
601 hyporheic exchange needs to be modeled accurately as it represents a significant portion of
602 stream CO₂ contributing 47% in the East River. Finally, through the direct comparison of
603 existing statistical methods to the stream network model and sample data, we found that
604 statistical upscaling of *p*CO₂ can cause a significant overestimation of CO₂ fluxes within the East
605 River. Therefore, it is paramount that process-based models be applied at regional and global
606 scales to accurately constrain the river and stream CO₂ emissions.

607 **Acknowledgments and Data**

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611 paper. All data and code used in this work are available in the Supplemental Information for
612 reviewers to access; further, the dataset will be available by the time of publication in the ESS-
613 DIVE Database for public access, where it is currently under review.

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