A COINTEGRATION AND CLUSTERING BASED APPROACH TO PAIR TRADING OF STOCKS FROM SELECTED SECTORS OF THE INDIAN STOCK MARKET

Aayush Sahu-A22001

Anirudh Pratap Singh-A22007

Ashutosh Pradhan-A22011

Gopad Kumar Shukla-A22016

Saif Rizvi-A22028

Umesh Kumar Bugata-A22039

Advisor: Prof. Jaydip Sem

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Abstract

The project makes three distinct contributions. First, the work provides a cointegration-based pair trading strategy for stock portfolio creation, that can be used to earn profit by the investors in the stock market. Second, the pair-trading models are trained and tested on real-world stock market data, with the results displayed to illustrate the models' efficacy. Finally, since the stocks utilized in the pair trading portfolio designs are drawn from various National Stock Exchange (NSE) sectors, the outcomes of the pairings are an excellent signal of the possible profit that investors could make if they invest in those sectors using the recommended pair-trading technique.

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Chapter 1

Introduction

1.1 Stock Market

A stock market, stock market, or equity market is an aggregation of buyers and sellers of shares (also called shares) that represent ownership claims to businesses; they can include securities listed on a public stock exchange as well as stocks that are only traded privately, such as shares of private companies that are sold to investors through equity crowdfunding platforms. Investment is usually made with an investment strategy in mind.

Both "stock market" and "stock exchange" are often used interchangeably. Traders in the stock market buy or sell shares on one or more of the stock exchanges that are part of the overall stock market.

Stock markets provide a safe and regulated environment where market participants can confidently trade stocks and other eligible financial instruments, with zero to low operational risk.

Once new securities have been sold in the primary market, they are traded in the secondary market where one investor buys shares from another investor at the prevailing market price or at whatever price both the buyer and seller agree upon. The secondary market or the stock exchanges are regulated by

the regulatory authority. In India, the secondary and primary markets are governed by the Security and Exchange Board of India (SEBI).

A stock exchange facilitates stockbrokers to trade company stocks and other securities. A stock may be bought or sold only if it is listed on an exchange. Thus, it is the meeting place of the stock buyers and sellers. India's premier stock exchanges are the Bombay Stock Exchange and the National Stock Exchange.

As a primary market, the stock exchange allows companies to issue and sell their shares to the public for the first time through the initial public offering (IPO) process. This activity helps companies to raise the necessary capital from investors.

The company splits into several shares and sells some of those shares to the public at a price per share.

To facilitate this process, a company needs a marketplace where these shares can be sold, and this is achieved in the stock market. A listed company may also offer new, additional shares through other offers at a later stage, such as rights issues or follow-on offers. They can even buy back or remove their shares.

Investors will own a company's stock in the expectation that the stock will increase in value or receive a dividend payment, or both. The exchange acts as an intermediary in this capital-raising process and receives a fee from the company and its financial partners for its services.

Using exchanges, investors can also buy and sell securities they already own in the so-called secondary market.

1.2 Pairs Trading

Pairs trading was first introduced in the mid-1980s by a group of technical analyst researchers in Morgan Stanley, a multinational investment bank and

financial services company. The pairs trading strategy uses statistical and technical analysis to find potential market-neutral profits.

A market-neutral strategy is a type of investment strategy undertaken by an investor or an investment manager that seeks to profit from both increasing and decreasing prices in one or more markets while also attempting to completely avoid some specific form of market risk.

Market-neutral strategies are often attained by taking matching long and short positions in different stocks to increase the return from making good stock selections and decreasing the return from broad market movements.

Pair trading is a market-neutral strategy to identify and pair two stocks, usually from the same sector or industry, that show identical positive movements. When the move breaks down, the two stocks deviate from the path, causing a spread that becomes a trading opportunity.

In pair trading, you buy the better-performing stock and sell the other one when that trading opportunity comes up to balance the profit and loss. The direction of the broad market does not affect the loss or profit of the trade's strategy. Traders tend to lose less when trading pairs when they thoroughly understand and use pair-trading strategies.

1.3 Correlation and Co-integration

A pair trading strategy is based on the historical correlation of two securities. The securities in the pair trade must have a high positive correlation, which is the main driver of the strategy's profits. A pair trading strategy is best deployed when a trader identifies a correlation discrepancy. Relying on the historical notion that two securities will maintain a specified correlation, a pair trade can be placed when that correlation fluctuates.

Example: imagine that the historical price movements of HDFC Bank (HDFCBANK) and SBI (SBIN) show a high degree of positive correlation. If a price divergence were to occur, such that the correlation temporarily burst,

traders using the pairs approach could see this as an opportunity to deploy a spread.

When trading stocks and futures, pairs are most used. For the second group, the most famous pairs include oil versus natural gas, gold versus silver, wheat versus corn, and many others.

The basis of pair trades is that a strong positive or negative correlation has been established between them over a prolonged period. The ability to profit from a pair position depends on the belief that the pair will revert to its historical average after a temporary breakdown in correlation.

In principle, cointegration analysis can give traders more confidence that a temporary breakdown in correlation will indeed return to "normal" trading behavior.

Because of the strong correlation/cointegration that exists between the optimal pairs, there is theoretically less risk in these trade structures as compared to placing bare directional risk in a single underlying.

Chapter 2

Methodology

In this section, particulars of the data used and the methods employed in this work are described. Using training data from five NSE sectors, cointegrated stock pairs are first identified, and then portfolios are formed on those pairs. The pair-trading portfolios' yearly returns are calculated. The returns of the portfolios over the test period are used to compare the pairs and the sectors. As the part of research methodology, the following steps were involved

2.1 Sectors for analysis

From all the sectors listed in NSE and which are listed below, five have been chosen for analysis along with NIFTY 50 stocks. The sectors include – (i) Auto, (ii) IT, (iii) PSU, (iv) Bank, (v) FMCG, (vi) Media, (vii) Metal, (viii) Oil and Gas, (ix) Pharma. The top ten stocks from each sector have been taken for analysis based on their market capitalization.

2.2   Data Collection

Historical stock prices have been downloaded using the Yfinance library in Python which allows access to the Yahoo Finance API. As the training dataset, close values of the stock prices from '2018-1-1' to '2021-12-31' have been used. For evaluation, close values of the stock prices from '2022-1-1' to '2022-12-31' have been used as the test dataset.

2.3   Correlation Matrix

To obtain a comprehensive visualization of the correlation coefficients between the pairs of stocks in each sector, a correlation matrix is constructed for each sector at this stage using the heatmap function of the seaborn library. Given that a sector has ten stocks, Pearson's product-moment correlation coefficients will be available for 45 different pairs since each sector contains 10 stocks. The correlation coefficients are primarily calculated using the close prices' return values. Using the Python function pct-change function, the return series for each stock is calculated. The correlation coefficients can be used to estimate the degree of a linear relationship between two stocks, but they cannot detect whether there is cointegration between the pairs.

2.4   Identification of Co integrated stock pairs

A pair of stocks are said to be cointegrated if they exhibit significant correlation in the long term. If two stocks are cointegrated, there exists some linear combination between the stocks that will vary around a mean(Quantopian Inc.). The coint function, which is part of the Python statsmodels module's stattools submodule, is used to determine whether pairings are cointegrated. The coint test's null hypothesis presupposes that a given pair, which is supplied as the function's two parameters, is not cointegrated (MacKinnon, 2012). Therefore, pairings are presumed to be cointegrated if their p-values fall below the cutoff of 0.05. To construct pair-trading portfolios, pairs for

which p-values are less than 0.05 are taken into consideration.

2.5   OLS regression models with the pairs

An ordinary least square (OLS) regression model is built for the pairs for which the cointegration test null hypothesis has been rejected (i.e., the pairs that display cointegration) in the preceding stage. Conventionally, the predictor (i.e., independent variable) in the OLS model is chosen to be the stock with the greater mean value of its close price. The model is constructed using the OLS function specified in the linear-model submodule of the Python statsmodels module. There are various parts to the OLS function's output. The following are a few of the most significant ones. (i) The hedge ratio and the p-value of its t-statistics, (ii) The p-value of the F-statistics, (iii) The prob. of the Omnibus test statistics, (iv) The value of the Durbin-Watson test statistics, (v) The prob. of the Jarque-Bera test statistics. The hedging ratio is the coefficient parameter, and the p-value of the predictor's t-statistics must be significant for the predictor to have a meaningful level of explanatory power for the target. For the regression model to make accurate predictions, the p-value of the F-statistic needs to be significant (lower than 0.05). To ensure that the predictor has a substantial impact on the target, the Omnibus test statistic should likewise have a significant p-value. To prevent autocorrelation among the residuals, the Durbin-Watson test statistic's value should be close to 2. There should not be any significant autocorrelation among the model residuals and the cointegrated pair of stocks should have significant p-values for the F-statistics and the Omnibus test. There is one more prerequisite for cointegration, though: the residuals must be stationary which would be checked in the next step.

2.6   Trading Signals for the pairs

This stage involves creating the trading signals for the pair after the cointegration for the pairs has been verified. This requires numerous further steps. First, the daily value of the ratio between the close value of the predictor time

series (also known as asset1) and the close value of the target (also known as asset2) is designed as a variable called ratio. Second, by deducting the mean value from each ratio value and dividing the result by the ratio values' standard deviation, the standardized values of the variable ratio are calculated. The standard deviation is added to and subtracted from the mean value, respectively, to determine the upper and lower bounds of the Z-scores for the ratio values. The maximum and lower bounds of the Z-score for the ratio are 1 and -1, respectively, because the mean value of the Z-scores is 0 and their standard deviation is 1. Third, the following six columns are now added to a pandas data frame called signals: Date, asset1 (time series of the close values of the first stock), asset2 (time series of the close values of the second stock), Z score (standardized values of the ratio), the upper limit (all entries are "1" under this column), lower limit (storing the lower limit of the Z scores), and date. The trading signals for asset1 are now developed using the Z-scores and their upper and lower bounds. Asset1 should be used with the short strategy if the Z-score at a point exceeds the upper limit; otherwise, the long strategy should be employed. Selling asset 1 is part of the short strategy, and increasing asset 1 purchases is part of the long plan. The signals data frame now includes a new column called signals1, with the values "-1" for short cases and "1" for long cases for asset1. The signals data frame for asset2 also gains a new column, signals2. Signals2 entries are different from Signals1 entries in terms of sign. At this stage, the data frame consists of the following columns - date, asset1, asset2, Z-score, upper limit, lower limit, signals1, and signals2.

2.7   Identifying the points of investment opportunities

Two further columns are added to the signals data frame to identify the portfolio positions, or the areas of undervalued investment opportunities, for the two companies. Column positions1 is added for the initial stock, or asset 1. The first-order difference of the singals1 column is used to calculate the items under this column. Like the first stock, column positions2 for the second stock is added based on the signals2 column's first-order difference values. If "0" is entered under positions1, it means that signals1's prior

and current values have not changed. A signal1 entry with a value of "1" denotes a change from "0" to "1," while one with a value of "-1" denotes a transition from "1" to "0." The entries in column position 2 are chosen similarly. Records with a positions1 value of "1" indicate a long trigger for asset 1, while records with a positions1 value of "0" suggest a short trigger. Signal1's value has changed from "0" to "1" when a record has a position1 entry of "1". So, asset1 has been given a long trigger. Similar to this, a position1 entry of "-1" indicates a short trigger. An input of "0" for position1 denotes that asset1 does not require action. Like position 2, entries of "-1", "1," and "0" denote a short trigger, a long trigger, or no action required for asset 2, respectively. During the portfolio testing phase, a graph is drawn to show the short and long trigger points for both stocks.

2.8 Computation of returns

The portfolio returns for the year 2021 are calculated in the final phase. On January 1, 2022, the pair-trading portfolio is started with a capital investment of 100000 units for each asset (i.e., a total investment of 200000 units). The entire holding values and cash amount for both stocks are added up for each day of the test period and kept in a variable called total portfolio value. To determine the profit (or loss) as of December 31, 2022, the overall portfolio value's excess (or deficit) over the total original investment of 200000 units is determined. Transaction costs are not considered in this calculation. The return on the portfolio is generated from the calculated profit.

Chapter 3

Results

3.1 Auto-Sector

3.1.1 Correlation

Correlation is the easiest approach to look for stock pairs that exhibit long-term similar behavior, which can be exploited to get pairs that give good profit for a given testing period. The Correlation matrix is given in 3.1. The stock pairs exhibiting a Pearson correlation coefficient of more than 0.5 are selected as the correlated stock pairs. The correlated stock pairs obtained with this selection criteria are:

- MARUTI, TVSMOTOR

- M& M, MARUTI

- HEROMOTOCOP, TVSMOTOR

- HEROMOTOCOP, MARUTI

- EICHERMOTORS, MARUTI

- BHARATFORGE, TATMOTORS
- BAJAJAUTO, TVSMOTORS
- BAJAJAUTO, MARUTI
- BAJAJAUTO, HEROMOTOCOP
- AHSHOKLEY, BHARATFORGE

Figure 3.1: Correlation heat map with respective p-values

The 3.1 below gives the final value of the portfolio with the returns

Table 3.1: THE ANNUAL RETURNS OF THE PAIR-TRADING PORT-FOLIOS OF THE AUTO SECTOR STOCKS (PERIOD: JANUARY 1, 2022 - DECEMBER 31, 2022).

Stock pairs	Initial Investment	Final value	Profit	Return
MARUTI TVSMOTORS	200000	406406.45	6406.45	1.60
M& M MARUTI	200000	416955.32	16955.32	4.24
HEROMOTOCO TVSMOTOR	200000	441278.19	41278.19	10.32
HEROMOTOCOP EICHERMOTOR	200000	469844.07	69844.07	17.46
'BHARATFORG' MARUTI	200000	445110.83	45110.83	11.28
BHARATFORGE TATMOTORS	200000	348449.80	-51550.20	-12.89
BHARATFORG MARUTI	200000	433626.17	33626.17	8.41
BAJAJ AUTO TVSMOTORS	200000	393704.01	-6295.99	-1.57
BAJAJ AUTO MARUTI	200000	464142.30	64142.30	16.04
BAJAJ AUTO HEROMOTOCO	200000	431294.64	31294.64	7.82
ASHOKLEY BHARATFORGE	200000	444855.03	44855.03	11.21

3.1.2   Co-integration

As per the report published by the NSE on December 31, 2022, the ten most important stocks of the auto sector are as follows: Mahindra and Mahindra, Maruti Suzuki India, Tata Motors, Eicher Motors, Bajaj Auto, Hero Moto-Corp, Tube Investments of India, TVS Motor Company, Bharat Forge, and Ashok Leyland (NSE Website). Six pairs in this sector exhibited significant p-values for their cointegration, as depicted in 3.2 These six pairs are as follows:

- 'ASHOKLEY.NS', 'BHARATFORG.NS'

- 'ASHOKLEY.NS', 'EICHERMOT.NS'

- 'ASHOKLEY.NS', 'TVSMOTOR.NS'

- 'BHARATFORG.NS', 'EICHERMOT.NS'

- 'BHARATFORG.NS', 'TVSMOTOR.NS'

- 'EICHERMOT.NS', 'MandM.NS'

Figure 3.2: The matrix of the p-values of the cointegration tests for the pairs of stocks of the auto sector.

Due to space constraints, the results of the pair Ashok Leyland and Bharat Forge are presented in detail. For the other pairs, only the annual return figures for the year 2022 are presented. The daily close prices of Ashok Leyland and Bharat Forge are depicted for the training period (i.e., January 1, 2018, to December 31, 2021) in 3.3 to visually check the long-term association between them.

Figure 3.3: The plot depicting the daily close prices of the stocks Ashok Leyland (ASHOKLEY.NS) and Bharat Forge (BHARATFORG.NS), from January 1, 2018, to December 31, 2021.

Figure 3.4: The results of the OLS regression model with Bharat Forge as the target variable (denoted by asset2) and Ashok Leyland as the predictor variable (denoted by asset1).

Figure 3.5: The residual plot for the OLS regression model with Bharat Forge as the predictor and Ashok Leyland as the target variable.

The OLS regression results with Bharat Forge as the target and Ashok Leyland as the predictor variable are presented in 3.4. The hedge ratio (i.e., the coefficient parameter for Ashok Leyland) is found to be 5.6851 with a standard error of 0.017. The highly significant p-value of the F-statistic indicates that there is a strong linear relationship between the two series. The Jarque-Bera test yielded a weakly significant p-value for the test statistic indicating the skewness and the kurtosis of the residuals of the model are not like those of a normal distribution. The Durbin-Watson test statistic lies between 0 and 2 indicating a positive autocorrelation among the residual. Finally, the Omnibus test results support the p-value of the F statistic indicating the presence of a strong linear relationship between the target and the predictor. In the next step, the residuals of the model are computed and plotted. 3.5 depicts the residual plot which looks like a stationary series.

The Augmented Dickey-Fuller (ADF) test on the residual series yielded a value of -4.3084 while the critical value at the 1% level of significance is -3.4392 (Dickey & Fuller, 1979). The results of the ADF test indicated that the residual series is not stationary. However, as the Bharat Forge and Ashok Leyland series are cointegrated, we proceed to execute their pair-trading strategies. 3.6 depicts the plot of the Z-values of the ratio series and their upper and lower limits. The ratio series represents the ratio of the daily close prices of Bharat Forge and Ashok Leyland for the test data

Figure 3.6: The plot of the Z-values of the ratio series for the Bharat Forge – Ashok Leyland pair and their upper and lower limits.

The pair-trading signal points are plotted in 3.7, in which four types of signal points are identified, long strategy for Bharat Forge, short strategy for Bharat Forge, long strategy for Ashok Leyland, and short strategy for

Figure 3.7: The pair-trading scenarios for the stocks Bharat Forge and Ashok Leyland – the trading signals and their positions identified.

Figure 3.8: The plot of the daily value of the pair-trading portfolio of Bharat Forge and Ashok Leyland from January 1, 2022, to December 31, 2022.

Ashok Leyland. The four strategies are denoted by different symbols in 3.7. Finally, with an initial investment of 200000 units of capital for each of the two stocks, the trading strategy is initiated on January 1, 2022. 3.8 depicts the daily values of the portfolio for the year 2022. The value of the portfolio at the end of the year is found to be 444845 which corresponds to an annual return of 11.21%. 3.2 presents the annual returns for six pairs of stocks from the auto sector which exhibited significant p-values for their cointegration. Except for two, all the pairs are found to produce positive returns with the Ashok Leyland – Eicher Motors pair producing the highest return.

Table 3.2: THE ANNUAL RETURNS OF THE PAIR-TRADING PORT-FOLIOS OF THE AUTO SECTOR STOCKS (PERIOD: JANUARY 1, 2022 - DECEMBER 31, 2022).

Stock pairs	Initial Investment	Final value	Profit	Return
ASHOKLEY 'BHARATFORG'	200000	444855.02	44855.02	11.21
'ASHOKLEY' 'EICHERMOT'	200000	482467.33	82467.33	20.62
'ASHOKLEY' 'TVSMOTOR'	200000	358160.46	-41839.54	-10.46
'BHARATFORG' 'EICHERMOT'	200000	440510.21	40510.21	10.13
'BHARATFORG' 'TVSMOTOR'	200000	397865.59	-2134.41	-0.53
'EICHERMOT' 'MandM'	200000	425700.04	25700.04	6.425

3.1.3   Clustering

K-means clustering
The KMeans module has been imported from the sklearn.cluster package in
Python to perform the clustering. To find the optimum number of clusters
in the k-means technique we look at the silhouette score for different values
of K (no. of clusters)as shown in 3.9. The y-axis denotes silhouette scores
and the x-axis denotes the number of clusters (k values)

Figure 3.9: Silhouette score vs. number of clusters

The silhouette score maximizes at k=3. Hence, the number of clusters chosen
is 3.

The clusters were visualized using "k-means cluster centers" and the scatter
plot. The cluster centroids could be seen as green squares, and the number
of stocks associated with each cluster could be seen as circles around squares
with distinct colors. We can see three clusters in 3.10.

Figure 3.10: The results of K-means clustering

The number of stocks in each cluster can be further visualized using bar chart
-

Figure 3.11: Number of stocks in different clusters

The chart shown in 3.11 clearly shows that there are 7,2 and 1 stocks in
clusters 0,1 and 2 respectively.

Hierarchical clustering

The best way to visualize an agglomerative clustering algorithm is through a dendrogram, which displays a cluster tree, the leaves being the individual stocks and the root being the final single cluster.3.12 shows one such dendogram. The "distance" between each cluster is shown on the y-axis, and thus the longer the branches are, the less correlated two clusters are. To perform this clustering and visualize dendrogram, linkage, ward, and AgglomerativeClustering modules were imported.

For Auto Sector the dendrogram plot is shown in 3.12 –

Figure 3.12: Stocks Dendrogram

Three clusters are formed as can be distinguished by the distinct colors. Further to visualize the clusters, Agglomerative Clustering() and scatter-plot were used specifying the number of clusters as 3. The plot looked like

Figure 3.13: Hierarchical Clustering

Similar to the plot of k-means clustering, we see that there are some distinct clusters separated by different colors.

Affinity Propagation

Affinity Propagation module has been imported from sklearn.cluster package in python in order to perform the clustering.

Figure 3.14: Clusters as per Affinity Propagation

Similar to the plot of k-means clustering, we see that there are some distinct clusters separated by different colors as shown in 3.14.

Figure 3.15: Estimated number of clusters using AP

Bar chart shown in 3.15 has been used to visualize the number of stocks in each cluster. There are 7,2 and 1 stocks in clusters 0,1, and 2 respectively.

Figure 3.16: Cluster member counts

Evaluation of Clusters for AUTO Stocks- The Silhouette Coefficient score for the three techniques are presented in the table 3.5 below –

Table 3.3: Cluster output for auto sector

KMeans	0.5978
Hierarchical	0.5978
Affinity Propagation	0.5978

From the silhouette scores above, we proceed with Affinity Propagation clustering as the score is highest for Affinity Propagation. As the next step, we proceed with forming the stock pairs from different clusters as shown below. All the stock pairs from all the clusters are depicted below-

For cluster 0 stock pairs are-

- ASHOKLEY,TATAMOTORS

For Cluster 1 stock pairs are-

- MARUTI, TVSMOTOR
- M&M, TVSMOTOR
- Ma&M, MARUTI
- HEROMOTOCO, TVSMOTOR
- HEROMOTOCO, MARUTI
- HEROMOTOCO, M&M
- EICHERMOT, TVSMOTOR
- EICHERMOT, MARUTI
- EICHERMOT, M&M
- EICHERMOT, HEROMOTOCO

- BHARATFORG, TVSMOTOR

- BHARATFORG, MARUTI

- BHARATFORG, M&M

- BHARATFORG, HEROMOTOCO

- BHARATFORG, EICHERMOT

- BAJAJ-AUTO, TVSMOTOR

- BAJAJ-AUTO, MARUTI

- BAJAJ-AUTO, M&M

- BAJAJ-AUTO, HEROMOTOCO

- BAJAJ-AUTO, EICHERMOT

- BAJAJ-AUTO, BHARATFORG

There are no pairs formed in cluster 2 as there is only one stock present in cluster 2.

Cluster Evaluation using K-Means

Here we observe how different stocks in a cluster vary with time. It is noticeable that the stocks belonging to one cluster show similar behavior.

For Cluster 0

Figure 3.17: Stock time series for cluster 0

For Cluster 1

Figure 3.18: Stock time series for cluster 1

For Cluster 2

Figure 3.19: Stock time series for cluster 2

The purpose of clustering was to verify the results of co-integration which means we must look for the pairs of stocks formed common in co-integration and clustering. Following were the common pairs of stock for NIFTY-50-

BHARATFORG, EICHERMOT, BHARATFORGE, TVSMOTOR, EICHERMOT, MandM

Common Pair Visualization using TSNE -

Figure 3.20: TSNE visualization of validated pairs

3.2 IT-Sector

3.2.1 Co-integration

Information Technology (IT) sector:

As per the report published by the NSE on December 31, 2022, the ten most important stocks of the IT are as follows: Tata Consultancy Services, Infosys, HCL Technologies, Wipro, Tech Mahindra, LTIMindTree, Persistent Systems, MphasiS, Coforge and L&T Technology Services (NSE Website). 3.21 depicts the matrix of the p-values of the co-integration tests for each pair of IT sector stocks. As depicted in 3.21, three pairs exhibited significant p-values for their co-integration. These three pairs are as follows:

- HCLTECH.NS,INFY.NS

- INFY.NS, TCS.NS

- LTTS.NS,TECHM.NS

Figure 3.21: The matrix of the p-values of the cointegration tests for the pairs of stocks of the IT sector.

The results for the pair HCL Technologies – Infosys are presented in detail. Figure 1-9 exhibits the close values of the HCL and the Infosys series from January 1, 2018, to December 31, 2021. The results of the OLS regression model built with HCL Technologies as the predictor and Infosys as the target are presented in 3.23. The hedge ratio is 1.4341. The highly significant p-value of the F-statistics indicates that there is a strong linear relationship between the two series.

Figure 3.22: The plot depicting the daily close prices of the stocks HCL Technologies (HCLTECH.NS) and Infosys (INFY.NS), from January 1, 2018, to December 31, 2021.

Figure 3.23: The results of the OLS regression model with Infosys as the target variable (denoted by asset2) and HCL Technologies as the predictor variable (denoted by asset1).

The OLS regression results with Bharat Forge as the target and Ashok Leyland as the predictor variable are presented in Figure 1-3. The hedge ratio (i.e., the coefficient parameter for Ashok Leyland) is found to be 5.6851 with a standard error of 0.017. The highly significant p-value of the F-statistic indicates that there is a strong linear relationship between the two series. The Jarque-Bera test yielded a weakly significant p-value for the test statistic indicating the skewness and the kurtosis of the residuals of the model are not like those of a normal distribution. The Durbin-Watson test statistic lies between 0 and 2 indicating a positive autocorrelation among the residual. Finally, the Omnibus test results support the p-value of the F statistic indicating the presence of a strong linear relationship between the target and the predictor. In the next step, the residuals of the model are computed and plotted. Figure 1-4 depicts the residual plot which looks like a stationary series.

Figure 3.24: The residual plot for the OLS regression model with HCL Technologies as the predictor and Infosys as the target variable.

Figure 3.25: The plot of the Z-values of the ratio series for the HCL Technologies – Infosys pair and their upper and lower limits.

The residuals of the OLS model are plotted in Figure 1-11. The Z-values of the ratio with their upper and lower bounds are depicted in 3.25

The ADF test on the ratio series yielded a test statistic value of -3.0944, while the critical value at the 1% level of significance is -3.4392. The ADF test results indicate that the residual series is not stationary. However, the pair trading strategy is executed since the two series were found to be co-integrated. The signal points of the pair trading during 2022 are depicted in 3.26. 3.27 exhibits the daily portfolio value for the pair for the year 2022. The total portfolio value for the HCL Technologies – Infosys pair at the end of 2022 is 440109.19. For an initial investment of 200000, the pair yields

Figure 3.26: The pair-trading scenarios for the stocks HCL Technologies and Infosys – the trading signals and their positions identified.

Figure 3.27: The plot of the daily value of the pair-trading portfolio of HCL Technologies and Infosys from January 1, 2022, to December 31, 2022.

a return of 10.03%. Table 1-2 presents the portfolio return for the three pairs from the IT sector. All the pairs have yielded positive returns with ('LTTS.NS', 'TECHM.NS') pairs producing the highest return.

Table 3.4: THE ANNUAL RETURNS OF THE PAIR-TRADING PORT-FOLIOS OF THE IT SECTOR STOCKS (PERIOD: JANUARY 1, 2022 - DECEMBER 31, 2022).

Stock pairs	Initial Investment	Final value	Profit	Return
HCLTECH INFY	200000	440109.19.02	40109.19	10.03
INFY TCS	200000	425684.03	25684.03	6.42
LTTS TECHMAHINDRA	200000	470378.45	70378.45	17.59

3.2.2   CLUSTERING

IT Sector stocks- Based on the NSE's report published on December 31, 2022, the fifty stocks that have the most significant contributions to the overall index of this sector are as follows: Tata Consultancy Services Ltd., Infosys Ltd., HCL Technologies Ltd., Wipro Ltd., Tech Mahindra Ltd., LTIMindtree Ltd., Persistent Systems Ltd., MphasiS Ltd., Coforge Ltd., L&T Technology Services Ltd. from (NSE Website).

K-means clustering – KMeans module has been imported from sklearn.cluster package in Python in order to perform the clustering. To find the optimum number of clusters in the k-means technique we look at the silhouette score for different values of K (no. of clusters) from 3.28. The y-axis denotes silhouette scores and the x-axis denotes the number of clusters (k values)

Figure 3.28: Silhouette score vs number of clusters

The silhouette score maximizes at k=2. Hence, number of clusters chosen are 2.

Clusters were be visualized using 'k-means cluster centers' and scatter plot. The cluster centroids could be seen as green squares, and the number of stocks associated with each cluster could be seen as circles around squares with distinct colors. We can clearly see two clusters in figure 3.29. The

Figure 3.29: The results of K-means clustering

number of stocks in each cluster can be further visualized using bar chart -

Figure 3.30: Number of stocks in different clusters

As per figure 3.30, there are 5, 5 stocks in clusters 0 and 1 respectively.

Hierarchical clustering – The best way to visualize an agglomerate clustering algorithm is through a dendrogram, which displays a cluster tree, the leaves being the individual stocks and the root being the final single cluster. The "distance" between each cluster is shown on the y-axis, and thus the longer the branches are, the less correlated two clusters are. To perform this clustering and visualize dendrogram, linkage, ward, and AgglomerativeClustering modules were imported.

For IT Sector the dendrogram is shown in figure 3.31 –

Figure 3.31: Stocks dendogram

Three clusters are formed as can be distinguished by the distinct colors. Further to visualize the clusters, Agglomerative Clustering() and scatterplot was used specifying the number of clusters as 3. The plot is given in 3.32

Figure 3.32: Hierarchical Clustering

Similar to the plot of k-means clustering, we see that there are some distinct clusters separated by different colors.

Affinity Propagation – Affinity Propagation() module has been imported from sklearn.cluster package in Python to perform the clustering.

Figure 3.33: Affinity Propagation

Similar to the plot of k-means clustering, we see that there are some distinct clusters separated by different colors.

Figure 3.34: Estimated number of clusters using AP are 3

A bar chart has been used to visualize the number of stocks in each cluster. There are 5,4 and 1 stocks in clusters 0,1, and 2 respectively which can be seen in figure 3.35.

Figure 3.35: There are 5,4 and 1 stocks in clusters 0,1, and 2 respectively

Evaluation of Clusters for NIFTY-50 Stocks- The Silhouette Coefficient score for the three techniques is presented in the table below –

Table 3.5: Cluster output for auto sector

K-Means	0.6151
Hierarchical	0.5718
Affinity Propagation	0.5718

From the silhouette scores above, we proceed with Affinity Propagation clustering as the score is highest for K-Means Clustering. As the next step, we proceed with forming the stock pairs from different clusters as shown below. All the stock pairs from all the clusters are depicted below-

For Cluster 0 stock pairs are-

- TECHM, WIPRO

- TCS, WIPRO

- TCS, TECHM

- INFY, WIPRO

- INFY, TECHM

- INFY, TCS

- HCLTECH, WIPRO

- HCLTECH, TECHM

- HCLTECH, TCS

- HCLTECH, INFY

For Cluster 1 stock pairs are-

- MPHASIS, PERSISTENT

- LTTS, PERSISTENT

- LTTS, MPHASIS

- LTIM, PERSISTENT

- LTIM, MPHASIS

- LTIM, LTTS

- COFORGE, PERSISTENT

- COFORGE, MPHASIS

- COFORGE, LTTS

- COFORGE, LTIM

Cluster Evaluation using K-Means

Here we observe how different stocks in a cluster vary with time. It is noticeable that the stocks belonging to one cluster show similar behavior.

Figure 3.36: Stock Time-series for clutter 0

Figure 3.37: Stock Time-series for cluter 1

Figure 3.38: Common Pair Visualization using TSNE

The purpose of clustering was to verify the results of co-integration which means we must look for the pairs of stocks formed common in co-integration and clustering. Following are the common pairs of stock for NIFTY-50 stocks-

(HCLTECH, INFY), (INFY, TCS)

Chapter 4

Conclusion and future scope of work

The results are concluded and summarized below

1. The analysis done here was presented for 4 year time period which was chosen on elaborate analysis. The testing period encompassed the whole of the year 2022. 4 years before this was taken as the training period.x

2. The correlated pairs with Pearson correlation greater than 0.5 were taken as correlated stock pairs. For these pairs for 11 different sectors, the analysis was done on profit/loss calculation. For example, as given above, there are 11 correlated stock pairs, of which 2 exhibited negative ROI. Others gave a decent return. But, this may not always happen. For example, the IT sector showcased 6 correlated stock pairs of which 2 gave negative stock pairs

3. In the next step the Co-integrated stock pairs were identified. Co-integration looks into long-term correlation but very less or no correlation in a short period. With the Co-integrated stock pairs identified, the same profit loss calculation was done. For two sectors - Auto and IT the final portfolio value and ROI were presented. It was thus ob-

served that even though Co-integrated stock pairs exhibited negative ROIs. This can be attributed to the stochastic nature of the stock market. The training period and testing may exhibit completely different natures and as such stock pairs that would have been Co-integrated in the training may not exhibit the same behavior in the testing period

4. Analysis of 11 sectors revealed the following things.

   - 4 Sectors - Oil & Gas, Pharma, Media, and IT exhibited all positive returns. Oil & gas gave 2 stocks both of which were giving ROI of greater than 20. Media and IT gave 4 and 3 stock pairs respectively in the given training and testing period.

   - All the remaining sectors gave some negative ROI stock pairs too

   - Moreover in the Metal sector Hindalco and Tata Steel showcased a negative ROI of 24 which can be considered for future analysis.

   - Similarly, in FMCG Dabur and VBL exhibited the same behavior.

   - Apart from all these sectors Nifty50 was also considered. And there were 57 Co-integrated pairs of which 11 gave negative ROI, rest all gave positive ROI.

5. Another observation to shed light on is that the number of signals generated in a given year was 10-15. This means that the window of investment opportunities was limited to about 1 a month.

6. Finally, a clustering-based Co-integration approach was also used to arrive at a more reliable pair of stocks. This way the stock pairs were backed by the clustering.

7. The stock pairs identified as exhibiting erroneous behavior can be taken for further in-depth analysis which can shed more light on the stock market as well.

8. The study can be extended to inter-sectoral analysis as well as global stock markets.

9. With the knowledge of stock pairs a reliable investment strategy can be devised by integrating predictive algorithms like LSTM-based predictive models.

Chapter 5

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